

Search for CP-Violation in $K_S \rightarrow 3\pi^0$ decays

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On behalf of the NA48 Collaboration

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Motivation

- As you all know, CP-Violation in $K_L \rightarrow \pi\pi$ is firmly established ($\eta_{+-}, \eta_{00}, \epsilon'$)
- CP-Violation in $K_S \rightarrow 3\pi$ decays is equally allowed in the SM but has been investigated in much less detail owing to the difficulty of the measurement
- $CP(\pi^+\pi^-\pi^0) = -1$ ($L=0$) $+1$ ($L=1$) $CP(3\pi^0) = -1$
- The equivalent of η_{00} for $3\pi^0$ decays is:
 $\eta_{000} = A(K_S \rightarrow 3\pi^0) / A(K_L \rightarrow 3\pi^0)$
- Limits on η_{000} are still very poor
- In SM: $\eta_{000} = \epsilon + i \text{Im } a_1 / \text{Re } a_1 \sim \epsilon$

CP violation in $\pi^+\pi^-\pi^0$ and $3\pi^0$ decays

	Exp	Year	Technique	Result
η_{+-0}	FNAL-E621	1994	K_0 - K_0 bar incoherent	$\text{Im } \eta_{+-0} = -1.5 \pm 1.7 \pm 2.5 \times 10^{-2}$
	CERN- CPLEAR	1998	$p\bar{p} \rightarrow K^+ K_0 \bar{p} \pi^-$ $K^- K_0 \pi^+$	$\text{Re } \eta_{+-0} = -2 \pm 7^{+4}_{-1} \times 10^{-3}$ $\text{Im } \eta_{+-0} = -2 \pm 9^{+2}_{-1} \times 10^{-3}$
η_{000}	Barmin et al.	1983	Bubble ch.	$\text{Re } \eta_{000} = -8 \pm 18 \times 10^{-2}$ $\text{Im } \eta_{000} = -5 \pm 27 \times 10^{-2}$
	CPLEAR	1998	$p\bar{p} \rightarrow K^+ K_0 \bar{p} \pi^-$ $K^- K_0 \pi^+$	$\text{Re } \eta_{000} = 18 \pm 14 \pm 6 \times 10^{-2}$ $\text{Im } \eta_{000} = 15 \pm 20 \pm 3 \times 10^{-2}$
	Novosibirsk SND	1999	Tagged K_S $e\bar{e} \rightarrow \phi \rightarrow K_S K_L$	$\text{BR}(K_S \rightarrow 3\pi^0) < 1.4 \times 10^{-5}$ 90%CL

New Opportunity

- During Y2K NA48 did not have drift chambers because they were damaged by the beam pipe implosion...
- ...so we used excellent energy resolution of NA48 Lkr calorimeter and the NA48 beam line to improve $K_S \rightarrow 3\pi^0$
- Method:
 - The K^0 - K^0 bar incoherent mixture produced by 400 GeV protons on 40 cm long Be target
 - Look for K_S - K_L interference studying the intensity of $K \rightarrow 3\pi^0$ decays as a function of proper time
 - Measure the detector acceptance using $3\pi^0$ decays from a K_L beam (taken a month before)
 - Apply MC corrections to take into account the slight geometrical difference of the two beams

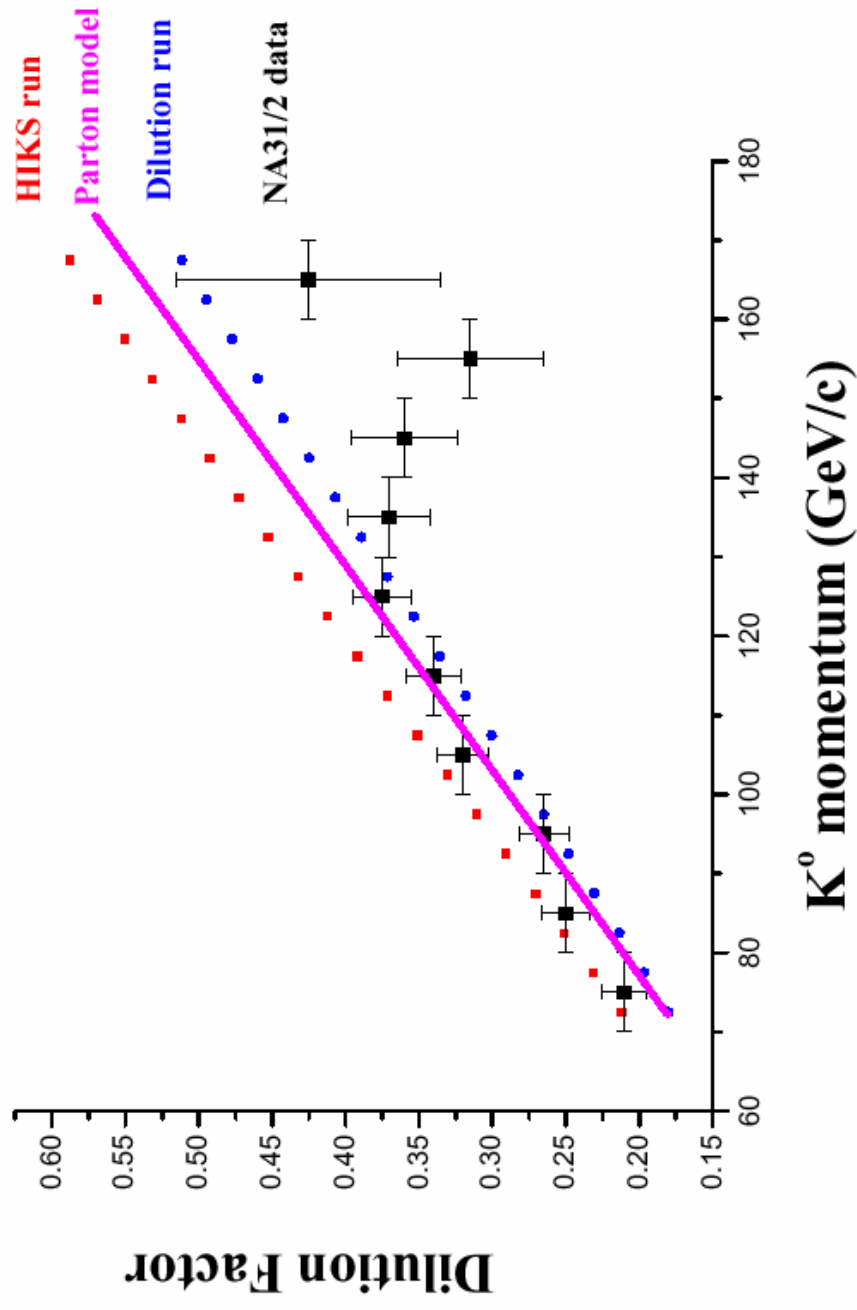
Fitted function

$$f(E, t) = \frac{NEAR}{FAR}$$

$$A(E) \left[1 + |\eta_{000}|^2 e^{(\Gamma_L - \Gamma_S)t} + 2D(E) e^{\frac{1}{2}(\Gamma_L - \Gamma_S)t} (\operatorname{Re}\eta_{000} \cos \Delta mt - \operatorname{Im}\eta_{000} \sin \Delta mt) \right]$$

$$D(E) = \frac{N_{K^0} - N_{\bar{K}^0}}{N_{K^0} + N_{\bar{K}^0}}$$

K^0 - K^0 bar Dilution



Data Taking

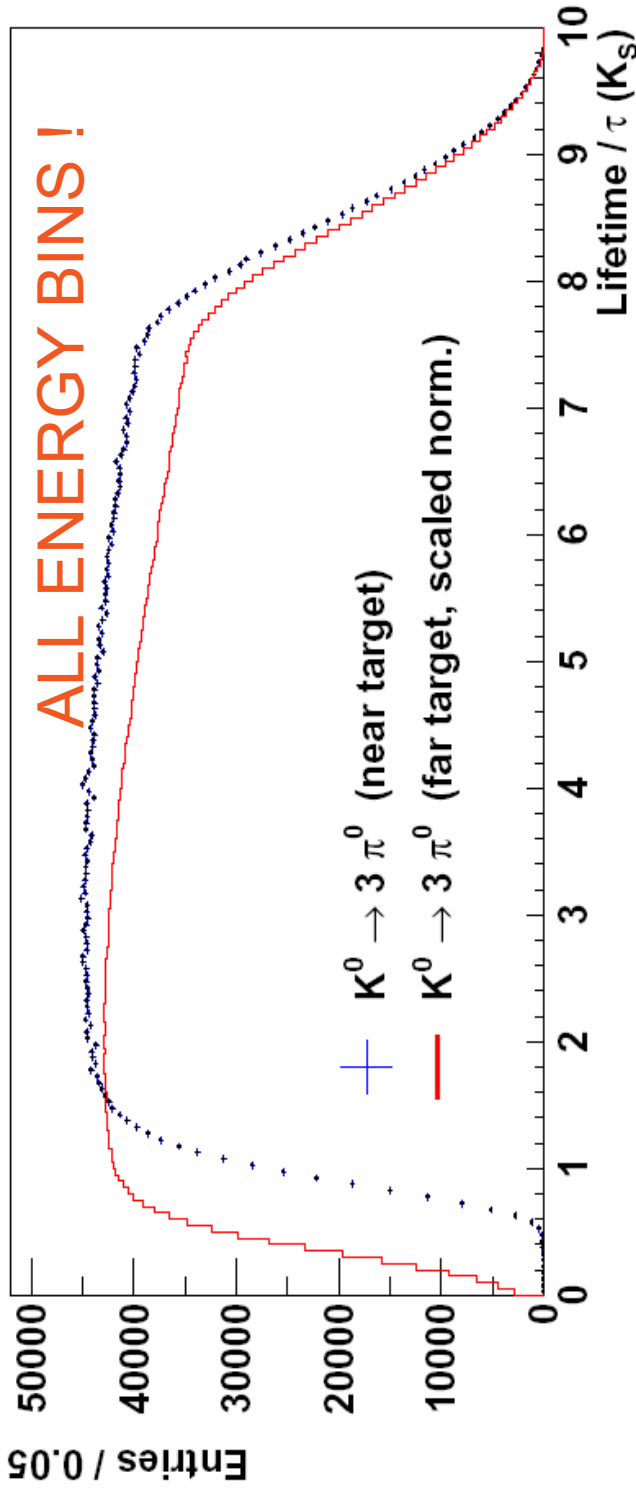
- We took data with the NEAR and far FAR beam configuration at different times
- Same trigger and detector
- We kept similar accidental activity adjusting the beam intensity
- P_{\dagger} (Energy centre of gravity) distribution of the two beams is different (unavoidable).

Data Taking Conditions

	P Energy (GeV)	Prod angle (mrad)	Beam length (m)	Dipole	Dates (Y2K)
FAR	450	2.4	120	ON	~15/6 ~15/7
NEAR	400	3.0	6	OFF	~20/7 ~28/8

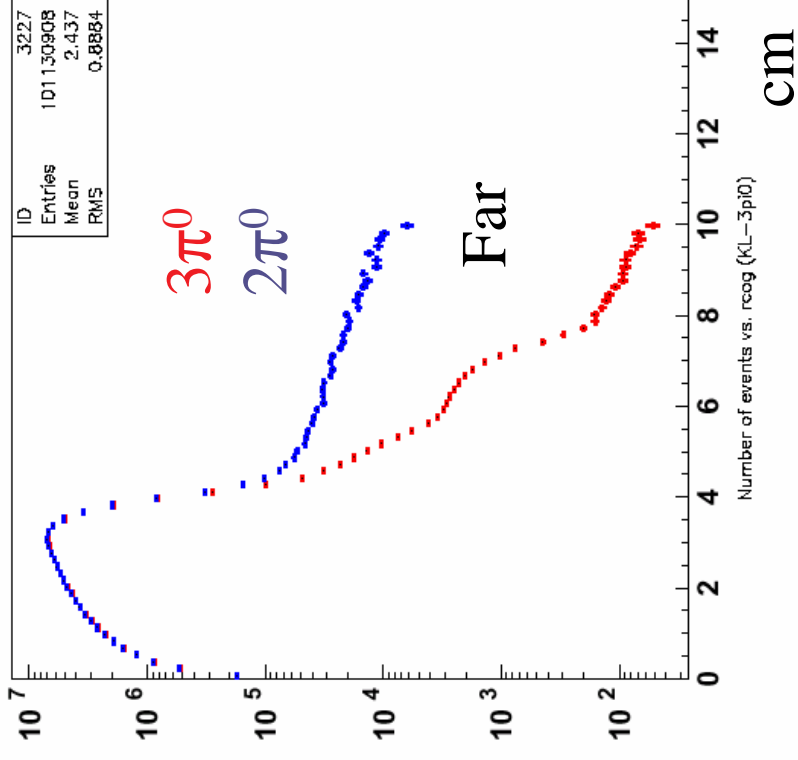
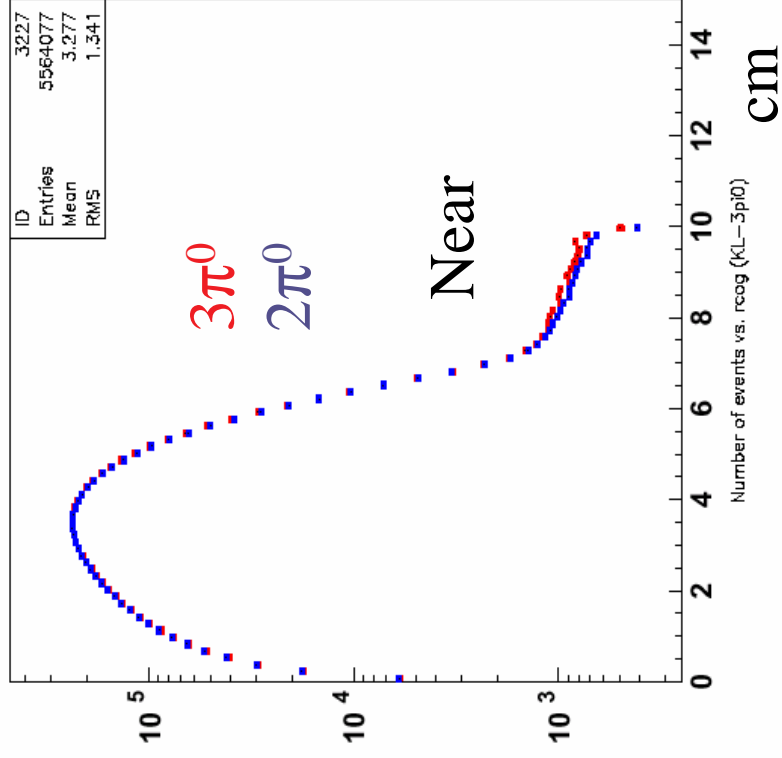
Data as a function of proper time

- Trigger efficiency: 99.7%
- Statistics from NEAR target: $\sim 5.6 \cdot 10^6 K \rightarrow 3\pi^0$
- Statistics from FAR target: $\sim 10^7 K_L \rightarrow 3\pi^0$

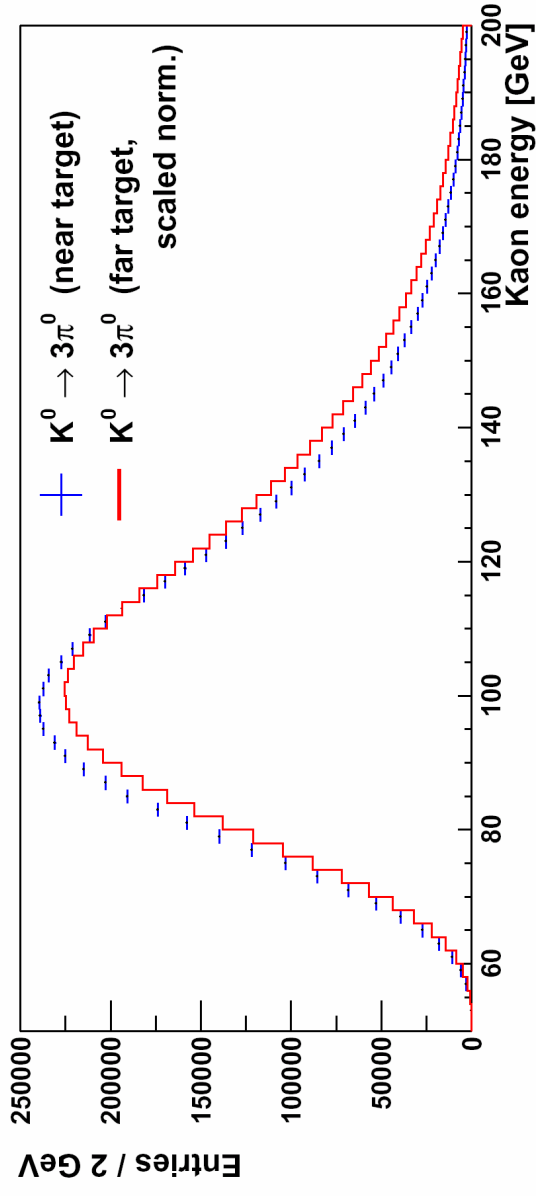


Energy Centre of Gravity

Normalised to $3\pi^0$ statistics



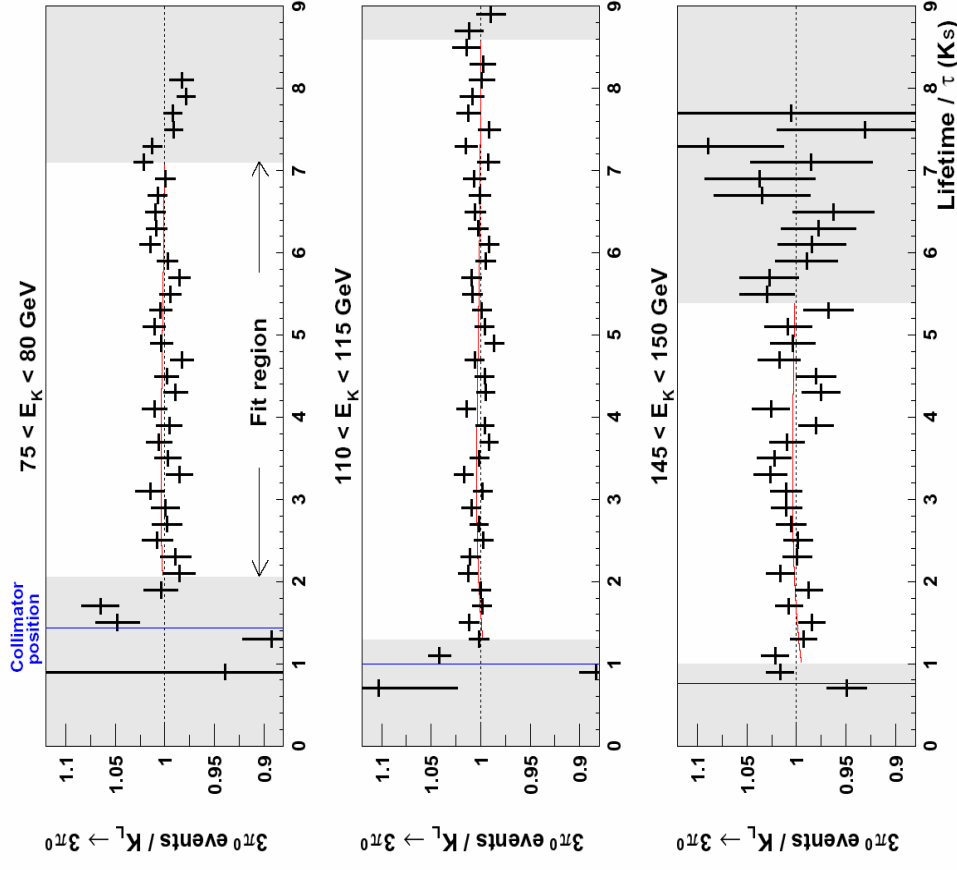
Kaon Energy distribution



- To take into account the slightly different kaon spectra, the analysis is done in bins of energy

NEAR/FAR data (MC corrected)

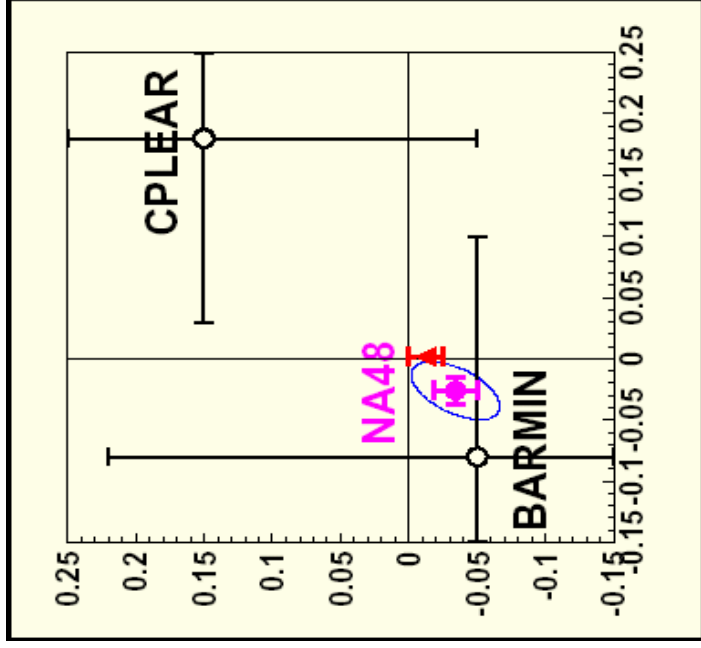
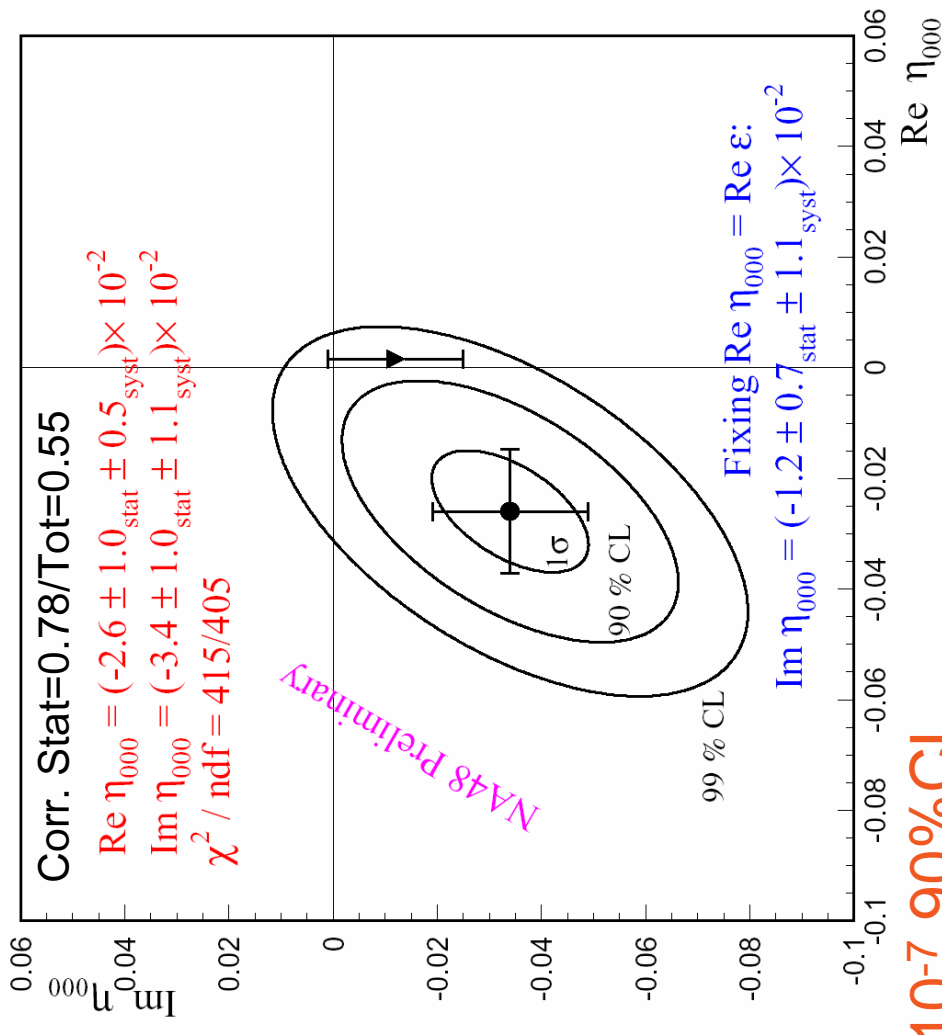
- The distribution as a function of proper time is shown for three different energy bins.
- For each energy bin, the NEAR/FAR event distribution is corrected for the FAR/NEAR Monte Carlo



Systematics

	Re η_{000} (10^{-2})	Im η_{000} (10^{-2})
Accidentals	± 0.1	± 0.6
Energy Scale	± 0.1	± 0.1
K^0 - K^0 bar Dilution	± 0.3	± 0.4
Acceptance	± 0.3	± 0.8
Binning	± 0.1	± 0.2
Total	± 0.5	± 1.1

Result of the fit



$$\text{BR}(K_S \rightarrow 3\pi^0) < 3.0 \cdot 10^{-7} \text{ 90\%CL}$$

Discussion

- The result is not only interesting as a test of CP conservation
- It also provides input to the **Bell-Steinberger unitarity relation**, improving by about 40% the error on the CPT-Violation parameter $\text{Im } \delta$

$$K_L \sim K_2 + (\varepsilon_k + \delta_k) K_1$$

$$K_S \sim K_1 + (\varepsilon_k - \delta_k) K_2$$

ε_k is CP - Violating and CPT - Conserving

δ_k is CP - and CPT - Violating

Bell-Steinberger relation

$$\left[-i(m_s - m_L) + \frac{1}{2}(\Gamma_s + \Gamma_L) \right] \langle L | S \rangle = \sum_f A(K_s \rightarrow f) A^*(K_L \rightarrow f)$$

$$\text{Re } \varepsilon_k - i \text{Im } \delta_k = \frac{1}{2 \left(i \Delta m + \frac{1}{2}(\Gamma_s + \Gamma_L) \right)} \sum_f A(K_s \rightarrow f) A^*(K_L \rightarrow f)$$

Error dominated by the poor knowledge of $A(K_s \rightarrow 3\pi^0)$

Conclusion

- $\text{Im } \delta = (-1.2 \pm 3.0) 10^{-5}$
- Previously: $\text{Im } \delta = (2.4 \pm 5.0) 10^{-5}$
- If CPT is conserved in the semi-leptonic K^0 decays the phase of δ is fixed and:

$$M_{K^0} - M_{\bar{K}^0} = (-1.7 \pm 4.2) \times 10^{-19} \text{ GeV}$$