

1                   **RECENT RESULTS ON DIRECT CP**  
2                   **VIOLATION FROM NA48 EXPERIMENT AT**  
3                   **CERN**

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11  
12                   The direct CP violation parameter  $\text{Re}(\varepsilon'/\varepsilon)$  has been measured from two-pion  
13                   decays of neutral kaons by the NA48 experiment at CERN SPS. The analysis  
14                   of a new data sample, collected in 2001 under different conditions compared  
15                   to earlier years (1997–99), provide the result:  $\text{Re}(\varepsilon'/\varepsilon) = (13.7 \pm 3.1) \times 10^{-4}$ .  
16                   Combining this result with that published from 1997–98-99 data, we obtain  
17                   an overall value  $\text{Re}(\varepsilon'/\varepsilon) = (14.7 \pm 2.2) \times 10^{-4}$  from the NA48 experiment.

18                   **1 Introduction**

19                   CP violation was discovered in the neutral kaon system in 1964 [1] with  
20                   the first observation of the CP-forbidden decay  $K_L \rightarrow \pi^+\pi^-$ . If CP were  
21                   conserved,  $K_S$  and  $K_L$  particles would be pure CP eigenstates, decaying  
22                   only into  $CP = +1$  and  $CP = -1$  final states, respectively. The observa-  
23                   tion of  $K_L \rightarrow 2\pi$  ( $CP = +1$ ) decays provides a clear evidence of CP non  
24                   conservation.

25                   The main component of CP violation is due to the mixing of the CP  
26                   eigenstates, called *indirect* CP violation and represented by the mixing  
27                   parameter  $\varepsilon$ . Another component, called *direct* CP violation and repre-  
28                   sented by the parameter  $\varepsilon'$ , may originate in the decay process through  
29                   the interference of amplitudes with different isospins.

30                   In the Standard Model of electro-weak interactions, CP violation origi-  
31                   nates from an irreducible complex phase in the quark mixing matrix [2].

32 Current theoretical predictions of  $\varepsilon'/\varepsilon$  range from  $\approx -10 \times 10^{-4}$  to  $\approx$   
 33  $+40 \times 10^{-4}$  [3].

The direct CP violation component is determined by measuring the double ratio  $R$  of partial decay widths, which is related to  $\varepsilon'/\varepsilon$  as follows<sup>1</sup>:

$$R \equiv \frac{\Gamma(K_L \rightarrow \pi^0\pi^0)/\Gamma(K_S \rightarrow \pi^0\pi^0)}{\Gamma(K_L \rightarrow \pi^+\pi^-)/\Gamma(K_S \rightarrow \pi^+\pi^-)} \simeq 1 - 6 \operatorname{Re}(\varepsilon'/\varepsilon) \quad (1)$$

34 Results on direct CP violation were published by two experiments in  
 35 1993: NA31 [4] measured  $\operatorname{Re}(\varepsilon'/\varepsilon) = (23.0 \pm 6.5) \times 10^{-4}$ , while E731 [5]  
 36 measured  $\operatorname{Re}(\varepsilon'/\varepsilon) = (7.4 \pm 5.9) \times 10^{-4}$ .

37 More recently, NA48 published the measurement [6]  $\operatorname{Re}(\varepsilon'/\varepsilon) = (15.3 \pm$   
 38  $2.6) \times 10^{-4}$ , obtained from the analysis of data collected in 1997 [7],  
 39 1998 and 99, and KTeV presented a preliminary value [8]  $\operatorname{Re}(\varepsilon'/\varepsilon) =$   
 40  $(20.7 \pm 2.8) \times 10^{-4}$  from data accumulated in 1996 [9] and 1997. These  
 41 results provide a convincing evidence of direct CP violation in the decay  
 42 of neutral kaons.

43 We report here a measurement of  $\operatorname{Re}(\varepsilon'/\varepsilon)$  performed by NA48 us-  
 44 ing the 2001 data sample, recorded in different experimental conditions  
 45 compared to earlier years. The main differences consist in the drift  
 46 chambers, rebuilt after the implosion of the beam tube in november  
 47 1999, and the SPS beam. Thanks to an extended SPS duty cycle, made  
 48 possible after the closure of LEP, data were taken at a 30% lower instan-  
 49 taneous beam intensity while keeping about the same per day statistics.

50 The 2001 data, equivalent to roughly half of the total 1998+99 statis-  
 51 tics, have been used to check the insensitivity of the result to intensity-  
 52 related effects and to complete the statistics for the final  $\operatorname{Re}(\varepsilon'/\varepsilon)$  mea-  
 53 surement.

## 54 2 The NA48 method

55 The double ratio  $R$ , from which  $\operatorname{Re}(\varepsilon'/\varepsilon)$  is derived, is measured by count-  
 56 ing the number of decays in each of the four decay modes. The experi-  
 57 ment is designed to obtain cancellation of systematic effects contributing  
 58 symmetrically to different components of the double ratio.

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<sup>1</sup>as the phase of  $\varepsilon'$  and that of  $\varepsilon(\simeq -\pi/4)$  are very close, we get  $\varepsilon'/\varepsilon \simeq \operatorname{Re}(\varepsilon'/\varepsilon)$ .

59 The sensitivity of the measurement to accidental activity and to vari-  
60 ations in beam intensity and detection efficiency is minimized by the si-  
61 multaneous collection of the four decay modes in the same decay region.  
62 Dead time conditions affecting any of the decay modes are recorded and  
63 applied offline to all modes. In order to eliminate the effect of the small  
64 and slow variations of the  $K_L$  and  $K_S$  beam intensities,  $K_S$  events are  
65 further weighted by the  $K_L/K_S$  intensity ratio.

66 Two nearly-collinear neutral beams, converging to the center of the  
67 electromagnetic calorimeter, provide  $K_L$  and  $K_S$  decays in the same fidu-  
68 cial region with similar momentum spectra. In order to be insensitive  
69 to residual differences in the beam momentum spectra, the analysis is  
70 performed in bins of kaon energy.

71 The difference between  $K_L$  and  $K_S$  acceptances, due to different mean  
72 decay lengths, is minimized by weighting the  $K_L$  decays as a function of  
73 their proper lifetime, such that the  $K_L$  decay distribution becomes simi-  
74 lar to the  $K_S$  one. The small remaining differences in beam divergences  
75 and geometries are taken into account using a Monte Carlo simulation.

76 Decays from the  $K_S$  beam are identified by a coincidence between  
77 the decay time and the registered times of the protons producing the  $K_S$   
78 beam.

79 Residual backgrounds which do not cancel in the double ratio are  
80 minimized by identifying the  $\pi^+\pi^-$  and  $\pi^0\pi^0$  decays with high-resolution  
81 detectors.

82 A detailed description of the NA48 experimental apparatus and of  
83 the analysis of 1998–99 data can be found in [6].

### 84 **3 Beams, detectors and triggers**

85 The NA48  $K_L$  and  $K_S$  simultaneous beams [10] are produced in two dif-  
86 ferent targets by 400 GeV/c protons from the same SPS beam, having a  
87 cycle time of 16.8 s and a spill length of 5.2 s.<sup>2</sup> The ratio of their inten-  
88 sities is stable within 10%. The  $K_L$  beam intensity in 2001, measured  
89 from the number of selected  $K_L$  decays as a function of time within the  
90 extraction, is shown in Fig. 1 together with the intensity measured on  
91 1999 data.

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<sup>2</sup>The beam momentum was 450 GeV/c, the cycle time 14.4 s and the spill length 2.4 s in the 1997, 1998 and 1999 runs.

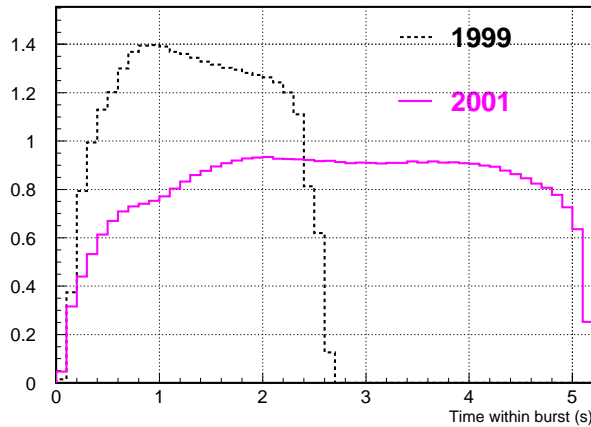


Figure 1: Rate of selected  $K_L$  events along the proton burst (in 0.1 s bins), proportional to the  $K_L$  beam intensity, in 2001 and 1999 data taking periods.

92 An array of scintillators [11] (Tagger) is used to record the time of  
 93 protons producing the  $K_S$  beam. An anti-counter [12] (AKS), formed by  
 94 a photon converter and three scintillation counters is located on the  $K_S$   
 95 beam at the beginning of the decay region.

96 Charged particles are measured by a magnetic spectrometer [13],  
 97 consisting of a dipole magnet giving a momentum kick of 265 MeV/c  
 98 and four drift chambers, with a momentum resolution  $\sigma_p/p = 0.48\% \oplus$   
 99  $0.009\% \times p/(1 \text{ GeV}/c)$ . A scintillator hodoscope composed of two planes of  
 100 orthogonal strips is located after the spectrometer to provide a precise  
 101 time measurement for charged particles. The signals from hodoscope  
 102 strips are combined in four quadrants by a fast logic electronics for the  
 103 first level of the  $\pi^+\pi^-$  trigger.

104 The energy, impact point and arrival time of photons from  $\pi^0\pi^0$  events  
 105 are measured by a quasi-homogeneous liquid krypton (LKr) electromag-  
 106 netic calorimeter [14] with a projective tower read-out. The energy reso-  
 107 lution is  $\sigma_E/E = 3.2\%/\sqrt{E} \oplus 9\%/E \oplus 0.42\%$  (E in GeV), the spatial reso-  
 108 lution better than 1 mm above 25 GeV.

109 An iron-scintillator hadron calorimeter is located downstream of the  
 110 electromagnetic calorimeter, followed by a muon counter made of three  
 111 planes of scintillator separated by 80 cm thick iron walls.

112 The beam intensities are measured by two beam counters, one of

113 which ( $K_L$  monitor) located at the end of the beam line, the other ( $K_S$   
114 monitor) near the target originating the  $K_S$  beam. Additional high-rate  
115 beam monitors have been installed before the 2001 run, the one for the  
116  $K_S$  beam located near the Tagger, allowing to measure beam structures  
117 down to  $\approx 200$  ns.

118 About  $4 \times 10^5$  particles per second reach the NA48 detectors. The  
119 trigger system is designed to reduce this rate to less than 10 kHz, with  
120 minimal loss from dead time and inefficiencies. The small inefficiencies  
121 of the main ( $\pi^+\pi^-$  and  $\pi^0\pi^0$ ) triggers are directly measured using data  
122 selected by redundant low-bias triggers. Other triggers, initiated by the  
123 beam monitors, are used to record the accidental activity with rates pro-  
124 portional to the  $K_L$  and  $K_S$  beam intensities.

125 The trigger for  $\pi^0\pi^0$  decays [15] makes use of the vertical and horizon-  
126 tal projections of the LKr calorimeter to reconstruct the total deposited  
127 energy, the longitudinal decay position and the extrapolated kaon im-  
128 pact point.

129 A two-level trigger system is used for the  $\pi^+\pi^-$  events. The first  
130 level reduces the rate to about 100 kHz using a coincidence of three  
131 fast signals: opposite quadrant coincidence in the scintillator hodoscope,  
132 hit multiplicity in the first drift chamber and total calorimetric energy  
133 above a threshold of 35 GeV. At the second level [16], a farm of asyn-  
134 chronous microprocessors performs a fast event reconstruction using  
135 data from the drift chambers and selects events compatible with a  $K \rightarrow$   
136  $\pi^+\pi^-$  decay.

## 137 4 Data analysis

### 138 4.1 Event selection

139 The  $K \rightarrow \pi^0\pi^0$  events are selected requiring four in-time photons de-  
140 tected by the electromagnetic calorimeter. From their measured ener-  
141 gies and impact points, the decay vertex position along the beam axis is  
142 reconstructed imposing that the four-photon invariant mass corresponds  
143 to the kaon mass. The invariant masses of the two photon pairs are then  
144 computed (with resolution better than 1 MeV/ $c^2$ ) and a  $\chi^2$  variable for the  
145  $\pi^0\pi^0$  hypothesis is calculated. A cut is applied on this variable in order  
146 to reject the residual background from  $K_L \rightarrow 3\pi^0$  events.

147 The  $K \rightarrow \pi^+\pi^-$  events are selected using informations from the spec-  
 148 trometer. Both the longitudinal and transverse positions of the decay  
 149 vertex can be determined, with resolutions of about 50 cm and 0.2 cm,  
 150 respectively. Since the beams are vertically separated by about 6 cm in  
 151 the decay region, a clean identification of the  $K_S$  and  $K_L$  decays is there-  
 152 fore possible using the reconstructed vertex position. A cut is applied on  
 153 the asymmetry  $\mathcal{A} = |p_1 - p_2|/(p_1 + p_2)$  between the two tracks momenta  
 154 in order to remove asymmetric decays in which one of the tracks could  
 155 be close to the beam pipe, where the Monte Carlo modelling is more dif-  
 156 ficult. Backgrounds from  $\Lambda \rightarrow p\pi^-$  and  $\bar{\Lambda} \rightarrow \bar{p}\pi^+$  are almost completely  
 157 eliminated by this cut.

158 Background from semileptonic  $K_L$  decays is strongly suppressed by  
 159 rejecting events with a track consistent with being either an electron or  
 160 a muon. Electrons are rejected by requiring the ratio  $E/p$  of the energy  
 161 deposited by the track in the LKr calorimeter over the track momentum  
 162 to be less than 0.8. Muons are rejected by requiring no in-time hits in  
 163 the muon counters near the track impact point. A further background  
 164 suppression is achieved by applying kinematic cuts on the two-pion in-  
 165 variant mass  $m_{\pi\pi}$  and on the kaon transverse momentum  $p'_T$ .

## 166 4.2 $K_S$ tagging

167 A decay is labeled  $K_S$  if a coincidence is found (within a  $\pm 2$  ns time inter-  
 168 val) between the event time and a proton time measured by the Tagger;  
 169 otherwise the decay is labeled  $K_L$ .

170 The time distributions for kaon decays to  $\pi^+\pi^-$  final states, identified  
 171 as  $K_S$  or  $K_L$  by their vertex position, is shown in Fig. 2. As tagging is the  
 172 only available way to distinguish  $K_S$  from  $K_L$  in  $\pi^0\pi^0$  decays, this method  
 173 is used for both  $\pi^0\pi^0$  and  $\pi^+\pi^-$  modes. The double ratio is therefore  
 174 sensitive only to differences in misidentification probabilities between  
 175 the two decay modes and not to their absolute values, so that systematic  
 176 effects are mostly symmetric.

177 The probability  $\alpha_{SL}$  that, due to coincidence inefficiencies, a  $K_S$  decay  
 178 is identified as a  $K_L$ , is called *tagging inefficiency*. In the  $\pi^+\pi^-$  mode  
 179 it is directly measured (using the vertical vertex position) to be  $\alpha_{SL}^{+-} =$   
 180  $(1.12 \pm 0.03) \times 10^{-4}$  and is found to be dominated by the Tagger inefficiency.

181 The difference between the tagging inefficiencies in  $\pi^+\pi^-$  and  $\pi^0\pi^0$   
 182 decays is estimated by comparing the time measurements obtained from

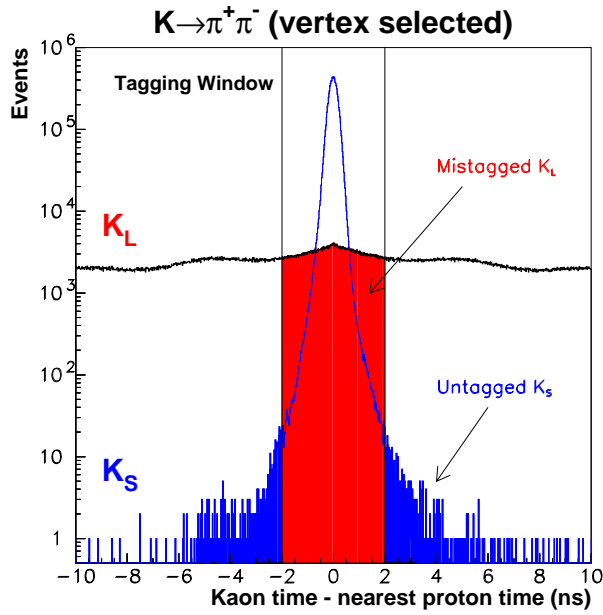


Figure 2: Time coincidence with nearest proton in the Tagger, for  $K_S$  and  $K_L$  decays to  $\pi^+\pi^-$  identified by their reconstructed vertex.

183 the LKr calorimeter and from the scintillator hodoscope in  $2\pi^0$  and  $3\pi^0$   
 184 events where one of the photons converts into an electron-positron pair.

185 The  $\pi^0\pi^0$  and  $\pi^+\pi^-$  tagging inefficiencies agree within an uncertainty  
 186 of  $\pm 0.5 \times 10^{-4}$ , corresponding to an uncertainty on  $R$  of  $\pm 3 \times 10^{-4}$ .

187 The probability  $\alpha_{LS}$  that, due to an accidental coincidence between  
 188 the event and a proton, a  $K_L$  decay is identified as a  $K_S$ , is called *ac-*  
 189 *cidental tagging*. It is measured in the  $\pi^+\pi^-$  mode and results to be<sup>3</sup>  
 190  $\alpha_{LS}^{+-} = (8.115 \pm 0.010) \times 10^{-2}$ .

191 The difference  $\Delta\alpha_{LS}$  between the  $\alpha_{LS}$  values in  $\pi^0\pi^0$  and  $\pi^+\pi^-$  decays  
 192 is determined by measuring the probability to find a proton within time  
 193 windows 4 ns wide, located before or after the event time in  $K_L$  events.

194 The resulting value of  $\Delta\alpha_{LS} \equiv \alpha_{LS}^{00} - \alpha_{LS}^{+-} = (+3.4 \pm 1.4) \times 10^{-4}$  corre-

<sup>3</sup>It was  $(10.649 \pm 0.008) \times 10^{-2}$  in the 1998–99 data sample.

195 sponds to a correction on  $R$  of  $(+6.9 \pm 2.8) \times 10^{-4}$ .

### 196 **4.3 Definition of the decay region**

197 Events are counted within the following fiducial ranges in kaon energy  
198  $E_K$  and proper time  $\tau$ :  $70 \text{ GeV} < E_K < 170 \text{ GeV}$ ;  $0 < \tau < 3.5\tau_S$ , where  
199  $\tau = 0$  corresponds to the position of the AKS counter and  $\tau_S$  is the  $K_S$  life-  
200 time. For  $K_L$  decays, the proper time cut is applied on the reconstructed  
201  $\tau$ , while for  $K_S$  the lower cut is applied using the AKS to veto decays oc-  
202 ccurring upstream. The nominal  $\tau = 0$  position defined by the AKS differ  
203 by  $21.0 \pm 0.5 \text{ mm}$  between  $\pi^+\pi^-$  and  $\pi^0\pi^0$  decays, resulting in a correction  
204 on  $R$  of  $(+1.2 \pm 0.3) \times 10^{-4}$ .

205  $K_S \rightarrow \pi\pi$  decays can be produced in both beams by scattering of beam  
206 particles in the collimators and, in the  $K_S$  case, in the AKS counter. To  
207 reduce this contamination, the extrapolated kaon impact point on the  
208 LKr calorimeter is required to be within 10 cm of the intersecting beam  
209 axes.

## 210 **5 Calculation of $R$ and systematic uncertainties**

211 The calculation of  $R$  is performed dividing the data into 20 bins in kaon  
212 energy, each bin 5 GeV wide. The numbers of  $K_S$  and  $K_L$  candidates,  
213 corrected for the mistagging probabilities, are shown in Table 1.

Table 1

Number of events (corrected for mistagging).		
	$\rightarrow \pi^0\pi^0$	$\rightarrow \pi^+\pi^-$
$K_L$	$1.546 \times 10^6$	$7.136 \times 10^6$
$K_S$	$2.159 \times 10^6$	$9.605 \times 10^6$

214 Corrections for trigger inefficiencies, background subtraction, and  
215 residual acceptance differences between  $K_S$  and  $K_L$  are applied sepa-  
216 rately in each energy bin before computing the average of  $R$ .

217 Corrections and systematic uncertainties from mistagging and AKS  
218 have already been discussed in the previous Section.



## 219 5.1 Trigger efficiencies

220 Events triggered by a scintillating fiber detector located inside the LKr  
221 calorimeter have been used to measure the  $\pi^0\pi^0$  trigger efficiency, which  
222 results to be  $(99.901 \pm 0.015)\%$ . As this efficiency is  $K_S - K_L$  symmetric,  
223 no correction to the double ratio needs to be applied.

224  $(98.697 \pm 0.017)\%$ . The difference in this efficiency between  $K_S$  and  
225  $K_L$  decays is computed in each energy bin, and the overall correction to  
226 the double ratio results to be  $(+5.2 \pm 3.6) \times 10^{-4}$ , where the uncertainty  
227 is given by the statistics of the control samples used to measure the  
228 efficiency.

## 229 5.2 Backgrounds

230 The only background affecting the  $K_L \rightarrow \pi^0\pi^0$  data comes from  $K_L \rightarrow 3\pi^0$   
231 decays, while the  $K_S$  mode is background free. The  $K_L \rightarrow 3\pi^0$  back-  
232 ground, uniformly distributed in the  $\chi^2$  variable, is estimated using a  
233 control region in the  $\chi^2$  distribution. The excess of  $K_L$  candidates in this  
234 region over a Monte Carlo expectation for  $\pi^0\pi^0$  decays is used to extrap-  
235 olate the background in the signal region. Background subtraction is  
236 performed in kaon energy bins; the overall correction to the double ratio  
237 is  $(-5.6 \pm 2.0) \times 10^{-4}$ .

238 Two control regions in the  $m_{\pi\pi} - p_T'^2$  plane are used to estimate the  
239 residual  $K_{e3}$  and  $K_{\mu3}$  backgrounds in the  $K_L \rightarrow \pi^+\pi^-$  sample. The back-  
240 ground distributions in these control regions are modelled by a  $K_{e3}$  sam-  
241 ple, selected with  $(E/p)_e > 0.95$ , and by a  $K_{\mu3}$  sample, obtained by re-  
242 versing the muon veto requirement. The tails in the  $K_L \rightarrow \pi^+\pi^-$  dis-  
243 tribution are estimated from the  $K_S$  sample. The result is then extrap-  
244 olated to the signal region, obtaining for the  $K_{e3}$  and  $K_{\mu3}$  background  
245 fractions the values  $10.5 \times 10^{-4}$  and  $3.0 \times 10^{-4}$ , respectively. These back-  
246 grounds are subtracted in kaon energy bins, resulting in a correction to  
247  $R$  of  $(+14.2 \pm 3.0) \times 10^{-4}$ .

248 In the  $K_S$  beam, the cut on the extrapolated kaon impact point is  
249 stronger than the  $p_T'^2$  cut applied to the  $\pi^+\pi^-$  events. As a consequence,  
250 beam scattering events are removed in the same way from both  $\pi^0\pi^0$  and  
251  $\pi^+\pi^-$  samples. On the contrary, in the  $K_L$  beam the  $p_T'^2$  cut applied only  
252 to the  $\pi^+\pi^-$  events is stronger, therefore a small residual contribution  
253 from scattering is left only in the  $\pi^0\pi^0$  sample. The correction for this  
254 effect is determined using  $K_L \rightarrow \pi^+\pi^-$  candidates with an inverted  $p_T'^2$

255 cut and applied in kaon energy bins. The resulting overall correction to  
256 the double ratio is  $(-8.8 \pm 2.0) \times 10^{-4}$ .

### 257 **5.3 Acceptance**

258 The difference between  $K_S$  and  $K_L$  acceptances is minimized (in both  
259 decay modes) by weighting  $K_L$  events according to their proper decay  
260 time.

261 The small residual difference, due to the different beam sizes and  
262 directions, is computed using a large-statistics Monte Carlo simulation  
263 ( $4 \times 10^8$  generated kaon decays per mode). The resulting correction to  $R$   
264 is  $(+21.9 \pm 3.5_{\text{MCstat}} \pm 4.0_{\text{syst}}) \times 10^{-4}$ .

### 265 **5.4 Event reconstruction**

266 Kaon energy, decay vertex and proper time in the  $\pi^0\pi^0$  events are de-  
267 termined using the photon energies and positions measured with the  
268 LKr calorimeter. The absolute energy scale is fixed using  $K_S \rightarrow \pi^0\pi^0$   
269 events and the known position of the AKL counter. Special runs (so-  
270 called  $\eta$  runs) with a  $\pi^-$  beam striking two thin targets located near the  
271 beginning and the end of the fiducial decay region have been used to  
272 cross-check the energy scale with two-photon decays of prompt  $\pi^0$  and  $\eta$   
273 mesons.

274 Linearity and spatial uniformity in the energy response are studied  
275 using  $K_{e3}$  decays, where the electron energy measured with the calorime-  
276 ter can be compared to the momentum measured with the spectrometer,  
277 and using data from  $\eta$  runs. Position measurements with the calorime-  
278 ter are also checked using  $K_{e3}$  data.

279 The total systematic error on the double ratio from the measurement  
280 of the photon energies and positions results to be  $\pm 5.3 \times 10^{-4}$ .

281 The uncertainty on  $R$  from the reconstruction of  $\pi^+\pi^-$  decays, due to  
282 uncertainties in the detector geometry, is estimated to be  $\pm 2.8 \times 10^{-4}$ .

### 283 **5.5 Intensity effects**

284 The accidental activity in NA48 detectors is mainly produced by kaon  
285 decays in the high-intensity  $K_L$  beam. The overlap of extra particles  
286 with a good event may result in the loss of the event at the trigger or

287 data analysis level. The effect on  $R$  is minimized by the simultaneous  
288 collection of the four decay modes and by the fact that  $K_S$  and weighted  
289  $K_L$  decays illuminate the detector in a similar way.

290 The possible residual effect can be separated into two components.  
291 The first one (intensity difference) is caused by intensity variations be-  
292 tween the two beams coupled to different, intensity-dependent, event  
293 losses in the  $\pi^+\pi^-$  and  $\pi^0\pi^0$  modes. The other one (illumination differ-  
294 ence) originates from a residual difference in the illumination between  
295  $K_S$  and  $K_L$  decays coupled to a dependence of the event loss probability  
296 on the impact points of the kaon decay products.

297 Assuming a linear dependence of the event loss probability on the  $K_L$   
298 beam intensity, the intensity difference effect is given by  $\Delta R = \Delta\lambda \times$   
299  $\Delta I/I$ , where  $\Delta\lambda$  is the difference between the mean losses in  $\pi^+\pi^-$  and  
300  $\pi^0\pi^0$  modes and  $\Delta I/I$  is the relative difference between the average  $K_L$   
301 beam intensity as seen by  $K_L$  and  $K_S$  events. The latter is measured in  
302 different ways: from detector activity within the readout time window  
303 before the event, from  $K_L$  beam monitor counts integrated over a 200 ns  
304 time window and from the correlation between  $K_S$  and  $K_L$  beams, com-  
305 puted using beam monitor counts taken at regular times during beam  
306 extraction. All methods agree with a zero result within a  $\pm 1\%$  uncer-  
307 tainty.

308  $\Delta\lambda$  is estimated by overlaying data and Monte Carlo events with  
309 events taken with the beam monitor trigger, and is found to be  $(1.0 \pm$   
310  $0.5) \times 10^{-2}$ , with a linear dependence on the beam intensity, as expected.  
311 The uncertainty on  $R$  from the intensity difference effects results to be  
312  $\pm 1.1 \times 10^{-4}$ , significantly better than in 1998–99 data due to the lower  
313 beam intensity and improved beam monitors.

314 The illumination difference effect is also estimated using the overlay  
315 technique. The corresponding uncertainty on the double ratio is evalu-  
316 ated to be  $\pm 3.0 \times 10^{-4}$ .

317 The effects of additional “in-time” detector activity, generated by the  
318 same collision in the  $K_S$  target producing the  $K_S$  event, are not taken  
319 into account by the methods described above. These effects have been  
320 studied mainly by searching, in  $\pi^0\pi^0$  events from pure  $K_S$  beam runs, for  
321 additional energy clusters in the LKr calorimeter. The effect on  $R$  is less  
322 than  $1 \times 10^{-4}$ .

323 **6 Results**

324 A summary of the corrections applied to  $R$  and of the systematic un-  
 325 certainties on the double ratio is shown in table 2, together with the  
 326 corresponding values obtained in the analysis of 1998–99 data [6].

Table 2

Corrections and systematic uncertainties on $R$ , in $10^{-4}$ units			
	2001	1998–99	
$\pi^+\pi^-$ trigger inefficiency	$5.2 \pm 3.6$	$-3.6 \pm 5.2$	(stat)
AKS inefficiency	$1.2 \pm 0.3$	$1.1 \pm 0.4$	
Reconstruction of $\pi^+\pi^-$	$\pm 2.8$	$2.0 \pm 2.8$	
Reconstruction of $\pi^0\pi^0$	$\pm 5.3$	$\pm 5.8$	
Background to $\pi^+\pi^-$	$14.2 \pm 3.0$	$16.9 \pm 3.0$	
Background to $\pi^0\pi^0$	$-5.6 \pm 2.0$	$-5.9 \pm 2.0$	
Beam scattering	$-8.8 \pm 2.0$	$-9.6 \pm 2.0$	
Accidental tagging	$6.9 \pm 2.8$	$8.3 \pm 3.4$	(stat)
Tagging inefficiency	$\pm 3.0$	$\pm 3.0$	
Acceptance (statistical)	<b><math>21.9 \pm 3.5</math></b>	$26.7 \pm 4.1$	(stat)
(systematic)	$\pm 4.0$	$\pm 4.0$	
Accidental activity:			
intensity difference	$\pm 1.1$	$\pm 3.0$	
illumination difference	$\pm 3.0$	$\pm 3.0$	(stat)
$K_S$ in time activity	$\pm 1.0$	$\pm 1.0$	
<b>Total</b>	<b><math>+35.0 \pm 6.5</math></b>	<b><math>+35.9 \pm 8.1</math></b>	<b>(stat)</b>
	$\pm 9.0$	$\pm 9.6$	

327 The residual acceptance correction is mostly due to beam geometry  
 328 effects and is well evaluated by Monte Carlo simulation. Some system-  
 329 atic uncertainties (indicated with “stat” in Table 2) are determined by  
 330 the statistical significance of the control sample used.

331 The final result from 2001 data is  $R = 0.99181 \pm 0.00147_{\text{stat}} \pm 0.00110_{\text{syst}}$ ,  
 332 corresponding to  $\text{Re}(\varepsilon'/\varepsilon) = (13.7 \pm 2.5_{\text{stat}} \pm 1.8_{\text{syst}}) \times 10^{-4}$ . This result is in  
 333 good agreement with the published value  $\text{Re}(\varepsilon'/\varepsilon) = (15.3 \pm 2.6) \times 10^{-4}$ ,  
 334 obtained from 1997–98-99 data at a different average beam intensity.  
 335 Taking into account the correlated systematic uncertainty of  $\pm 1.4 \times 10^{-4}$ ,  
 336 the combined final result from the NA48 experiment is  $\text{Re}(\varepsilon'/\varepsilon) = (14.7 \pm$   
 337  $2.2) \times 10^{-4}$ .

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