

# Recent Results on Radiative Kaon decays from NA48 and NA48/2.

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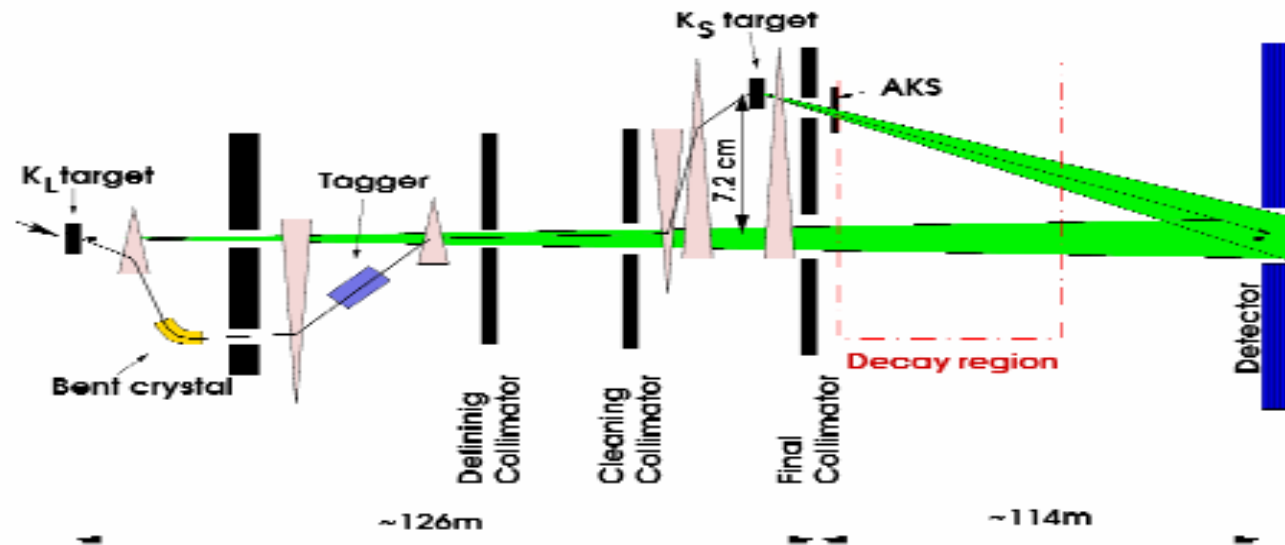
# Overview

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- Branching fraction of radiative decay  $K_L \rightarrow \pi^+ e^- \nu \gamma$  ( $K_L e3\gamma$ ) with respect to  $K_L e3$ 
  - Introduction
  - Selection and reconstruction
  - Results
- The radiative decay  $K^\pm \rightarrow \pi^\pm \pi^0 \gamma$ 
  - Introduction
  - Selection and reconstruction
  - Trigger
  - Background sources
  - Results
- Summary and Conclusions

# The $K_L e3\gamma$ decay. Introduction

- Dedicated run: 2 days in 1999 with only  $K_L$  beam



- $100 \cdot 10^6$  triggers recorded amounting to 2 TB

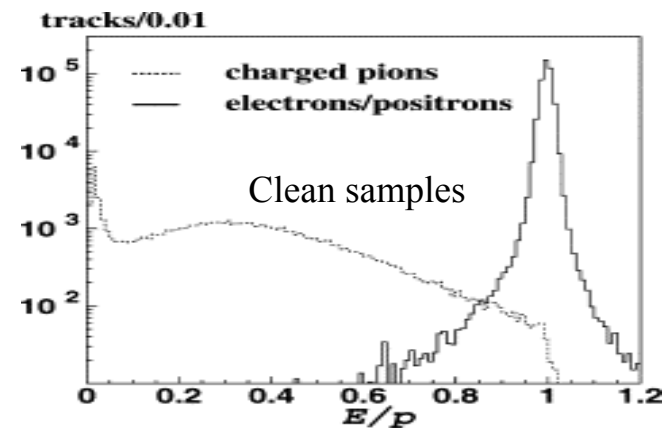
# The $K_L e 3\gamma$ decay. Introduction

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- Method: measure ratio of  $R = BR(K_L e 3\gamma) / BR(K_L e 3)$
- Two possible components for  $K_L e 3\gamma$ , IB and DE
  - IB comes from bremsstrahlung of electron
  - DE comes from weak vertex
- Due to small electron mass IB dominates
- IB has collinear and infrared singularities. Impose cuts on  $E_\gamma^*$  and  $\theta_{e\gamma}^*$   
 $R = BR(K_L e 3\gamma, E_\gamma^* > 30 \text{ MeV}, \theta_{e\gamma}^* > 20^\circ) / BR(K_L e 3)$
- Where  $BR(K_L e 3)$  includes any number of gammas

# Ratio of $BR(K_L e 3\gamma)/ BR(K_L e 3)$ . Selections.

- **Common** to both channels:
  - Two tracks from a good vertex. Distance between tracks @  $L_{Kr} > 25$  cm.
  - **Pion-electron separation** based on  $E/p$ . Final requirement  $0.93 < E/p < 1.1$  for electrons,  $E/p < 0.90$  for pions
  - Both of the possible  $p_K$  solutions must lie within  $(80, 160)$  GeV/c
  - Cuts against  $K_L \rightarrow \pi^+ \pi^- \pi^0$  and MUV against  $K\mu 3$ . Negligible background remains for  $K_L e 3$

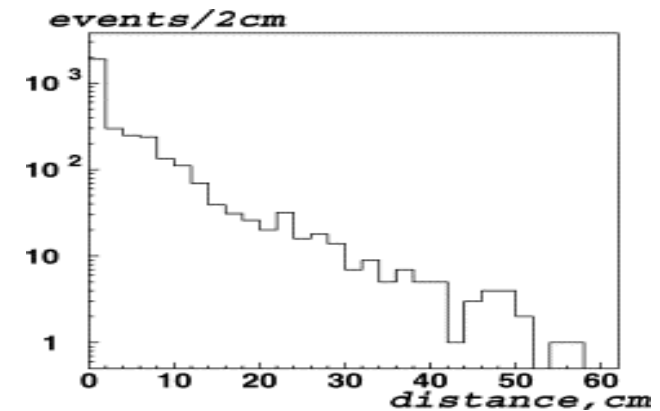


Select electron sample using hard cuts on  $E/p$  for pion

Select pion sample from  $K 2\pi$  or cutting hard on  $E/p$  for electron

# Ratio of $\text{BR}(\text{K}_L e 3\gamma) / \text{BR}(\text{K}_L e 3)$ . Selections.

- Specific to  $\text{K}_L e 3\gamma$ 
  - Require one cluster in time with  $E > 4 \text{ GeV}/c^2$
  - **Hadronic showers** can produce satellite clusters faking the radiated gamma. Distance between pion track at LKr and  $\gamma > 55 \text{ cm}$
  - Distance  $\gamma$ -e  $> 6 \text{ cm}$
  - Background dominated by  $\text{Ke}4 \sim 0.7 \%$
  - $E^* \gamma > 30 \text{ MeV}$  and  $\theta^*_{e\gamma} > 20^\circ$  for both solutions



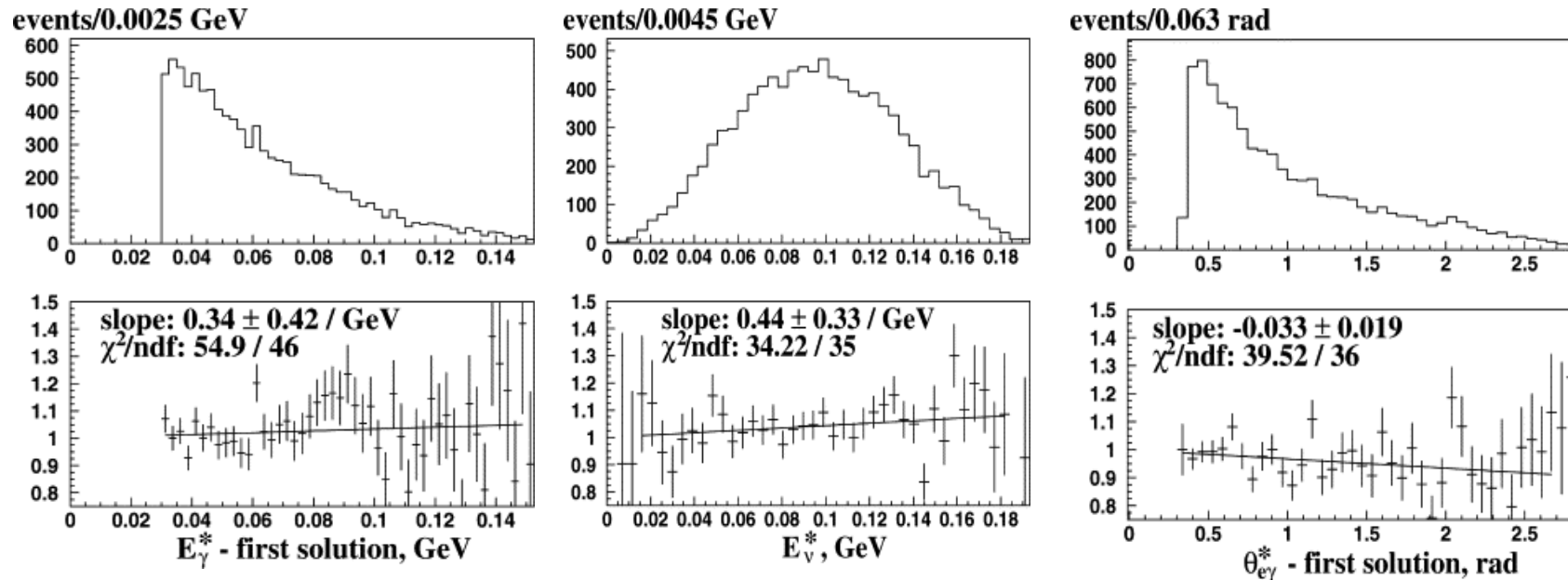
Select  $\text{K} \rightarrow \pi^+ \pi^-$ :

Distance between tracks at Lkr  $d_{\pi\pi} > 80 \text{ cm}$

Cluster energy  $E > 4 \text{ GeV}$

# The $K_L e 3\gamma$ decay. Data-MC comparison

- MC includes **radiative corrections**, virtual and real.  
Real: obtained using PHOTOS package.  
Virtual: Angular distribution of  $\theta_{e\gamma}^*$  used to weight MC accordingly to data
- Good agreement in relevant variables after weighting procedure



# The $K_L e3\gamma$ decay. Systematic checks

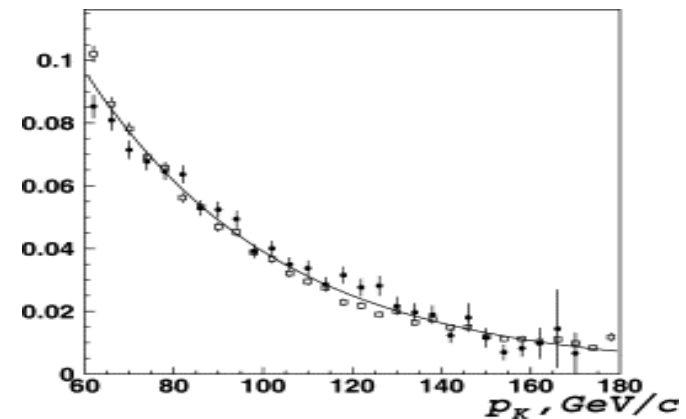
- Radiative corrections:
  - Rejection of more than one hard photon must be accounted for in MC
  - Correction of  $\sim 0.05\%$  due to differences in number of  $\gamma$  between data and MC
  - Requiring any number of hard  $\gamma$  agrees within  $0.2\%$

- Summary on systematic checks:

Source	$\Delta R/R$
$K_L$ spectrum	$+6_{-3} \cdot 10^{-3}$
$K_{e3\gamma}$ selection	$\pm 5 \cdot 10^{-3}$
$\gamma$ accidentals	$+2_{-1} \cdot 10^{-3}$
Background uncertainties	$+4_{-3} \cdot 10^{-3}$
$K_{e3}$ selection	$\pm 5 \cdot 10^{-3}$
Form-factor uncertainties	$\pm 1 \cdot 10^{-3}$
TOTAL	$+11_{-9} \cdot 10^{-3}$

- Main source of systematic uncertainty is **knowledge of kaon spectrum**

- Measurements from  $K2\pi$  and  $K3\pi$  and ‘diagonal solutions’ of  $K_L e3$
- Difference in acceptance ratio quoted a systematic uncertainty





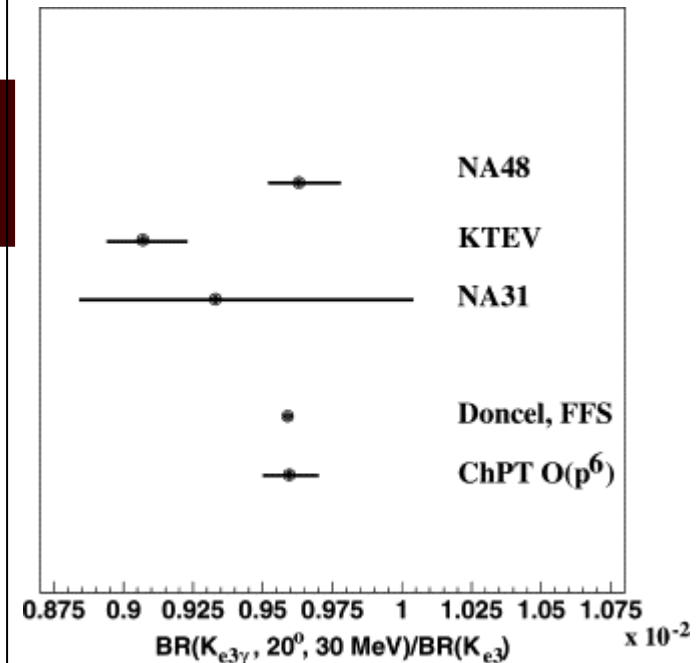
# The $K_L e3\gamma$ decay. Results

- Final sample 19000  $K_L e3\gamma$  and  $5.6 \cdot 10^6$   $K_L e3$  events

$$\frac{\text{BR}(K_L e3\gamma, E_\gamma^* > 30 \text{ MeV}, \theta_{e\gamma}^* > 20^\circ)}{\text{BR}(K_L e3)} = (0.964 \pm 0.008_{\text{stat}} \quad {}^{+0.011}_{-0.009 \text{ syst}})\%$$

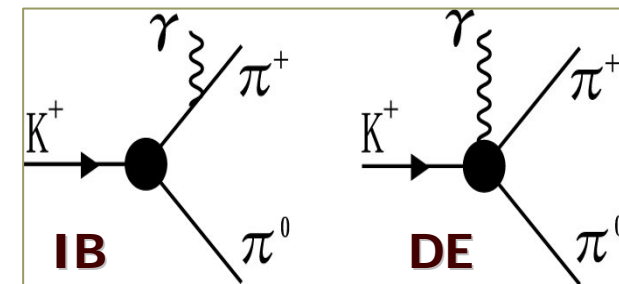
- Good agreement with theoretical predictions
- At a variance with another experimental results

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# The $K^\pm \rightarrow \pi^\pm \pi^0 \gamma$ decay. Introduction

- Two amplitudes:
  - Inner Bremsstrahlung (IB)
    - Calculable: QED corrections to  $K^\pm \rightarrow \pi^\pm \pi^0$
    - Suppressed by  $m_\pi$  and  $\Delta I=1/2$
  - Direct Emission (DE)
    - Insight on weak vertex structure
    - Electric (E) from  $L^4$  ChPT lagrangian and loops  $L^2$  (non predictable)
    - Magnetic (M) has contributions from chiral anomaly (calculable) and also direct contributions (non predictable)
- Interference (INT) possible between IB and electric part of DE
  - Measuring at the same time DE and INT gives measurement of both M and E
  - In addition CPV could appear in INT



PDG values for  $55 < T_\pi^* < 90$  MeV

BR(IB):  $(2.75 \pm 0.15) \cdot 10^{-4}$

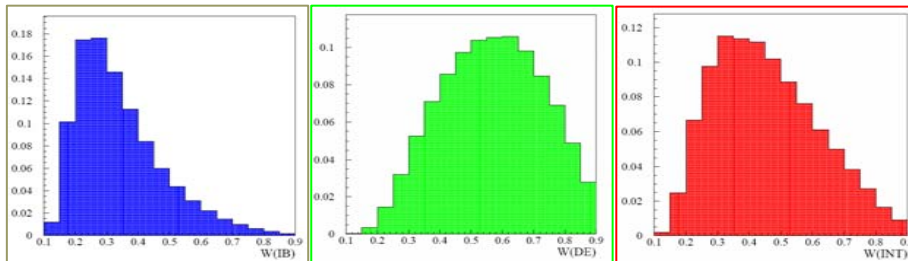
BR(DE):  $(4.4 \pm 0.8) \cdot 10^{-6}$

INT: not measured

# The $K^\pm \rightarrow \pi^\pm \pi^0 \gamma$ decay. Introduction

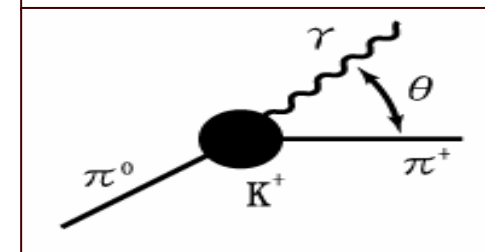
- Two Dalitz plot variables:  $W$  and  $T_\pi^*$

$$W^2 = \frac{(p_K p_\gamma)(p_\pi p_\gamma)}{m_\pi^2 m_K^2} \quad (\text{Lorentz invariant definition})$$



In K rest frame

$$W^2 = \frac{E_\gamma^2 (E_\pi - P_\pi \cos \theta_{\pi\gamma})}{m_K m_\pi^2}$$

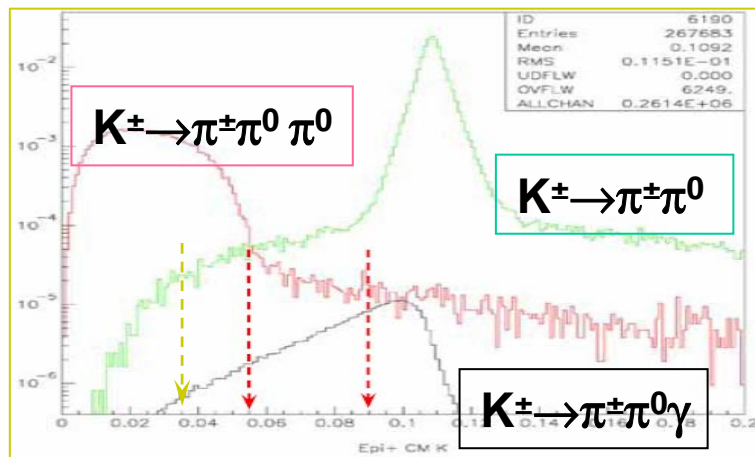


- Matrix element shows separation in  $W^2$  of components

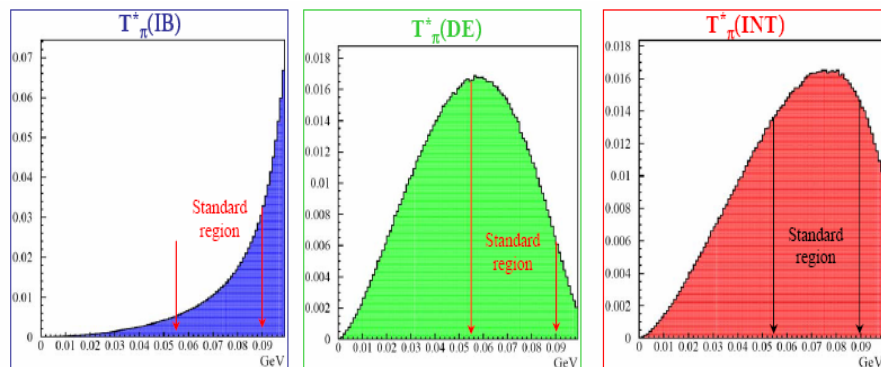
$$\frac{d\Gamma^\pm}{dW} \simeq \underbrace{\left(\frac{d\Gamma^\pm}{dW}\right)_{IB}}_{\text{IB}} \left[ 1 + \underbrace{2 \left(\frac{m_\pi}{m_K}\right)^2 W^2 |E| \cos((\delta_1 - \delta_0) \pm \phi)}_{\text{INT}} + \underbrace{\left(\frac{m_\pi}{m_K}\right)^4 W^4 (|E|^2 + |M|^2)}_{\text{DE}} \right]$$

# The $K^\pm \rightarrow \pi^\pm \pi^0 \gamma$ decay. Introduction

- Previous measurements:
  - $55 < T_\pi^* < 90$  MeV to avoid background from  $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$  and  $K^\pm \rightarrow \pi^\pm \pi^0$



- NA48/2: Enlarged  $T_\pi^*$  lower cut from 55 MeV to 0 MeV
  - Gain sensitivity to DE and INT
  - But must keep background from  $K^\pm \rightarrow \pi^\pm \pi^0 \pi$  under control !



- In NA48/2 cut at trigger level at  $\sim T_\pi^* < 90$  MeV

# The $K^\pm \rightarrow \pi^\pm \pi^0 \gamma$ decay. Introduction

- Previous measurements:
  - INT found to be compatible with zero

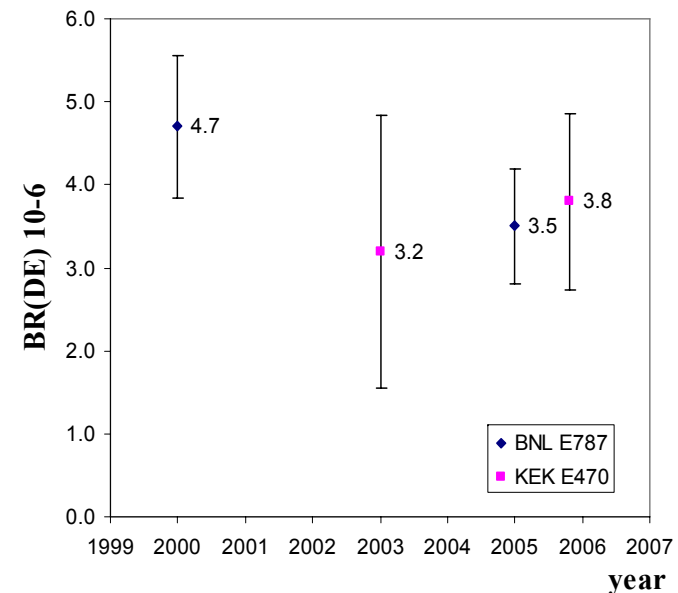
$$\text{INT} = (-0.58_{-0.83}^{+0.91})\% \text{ of IB} \quad \text{KEK E470}$$

$$\text{INT} = (-0.4 \pm 1.6)\% \text{ of IB} \quad \text{BNL E787}$$

- Set INT to zero and fit only to DE

Experiment	year	# of events	DE BR $10^{-6}$
Abrams [5]	1972	2100	$15.6 \pm 3.5 \pm 5.0$
Smith [18]	1976	2461	$23 \pm 32$
Bolotov [19]	1987	140	$20.5 \pm 4.6_{-2.3}^{+3.9}$
E787 [20]	2000	19836	$4.7 \pm 0.8 \pm 0.3$
E470 [21]	2003	4434	$3.2 \pm 1.3 \pm 1.0$
E787 [22]	2005	20571	$3.5 \pm 0.6_{-0.4}^{+0.3}$
E470 [23]	2005	10154	$3.8 \pm 0.8 \pm 0.7$

## Recent history of BR(DE)



- NA48/2 has analyzed > 5 times more events !

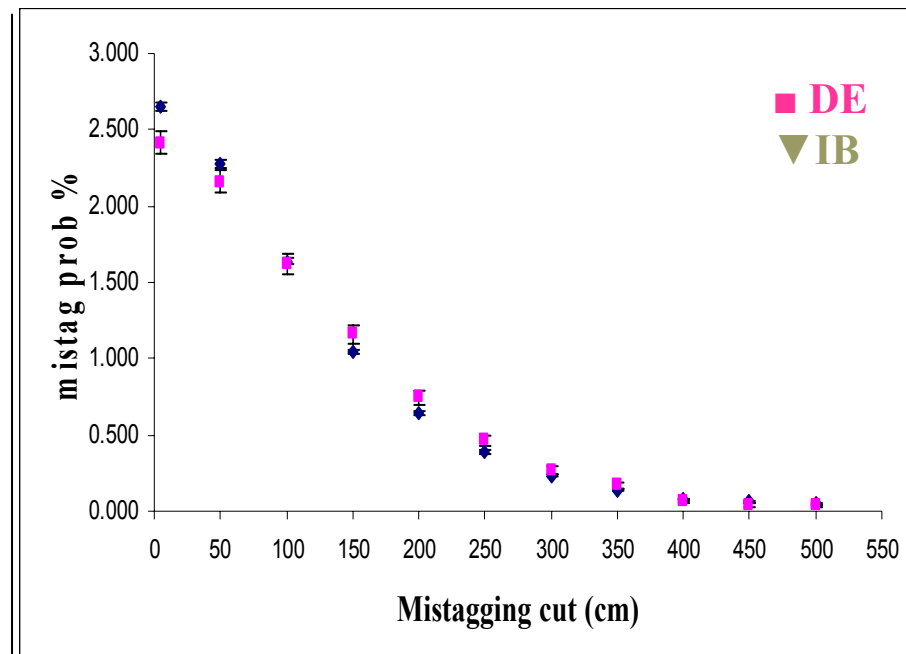
# The $K^\pm \rightarrow \pi^\pm \pi^0 \gamma$ decay. Reconstruction

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- Select 1 track and any number of clusters.
- Require 3 gammas with  $E_\gamma > 3$  GeV outside 35 cm radius from  $\pi$  at LKr. Gammas 10 cm away from other clusters
- **Charged vertex (zvc)**: Calculate the kaon decay point as the position where the  $\pi$  track intersects the beam line
- **Selecting the  $\gamma$  pairing for the  $\pi^0$** 
  - Three combinations are possible
  - Choosing the wrong combination for the  $\pi^0$  (**misstaggering**)  $\rightarrow$  choosing the wrong odd gamma  $\rightarrow$  Distorts  $E_\gamma \rightarrow$  distorts  $W$ .
  - Two possible methods used: Select the combination giving the best  $\pi^0$  invariant mass or combination giving the best kaon invariant mass
- **Neutral vertex (zvn)**: From imposing  $\pi^0$  mass to  $\gamma$  pairs. Must be in agreement with charged vertex (within 400 cm)

# The $K^\pm \rightarrow \pi^\pm \pi^0 \gamma$ decay. Reconstruction

- Miss tagging problem
  - Miss tagged events move to large  $W$
  - This could induce a DE component if difference between Data-MC
  - Must keep miss tagging probability as small as possible
- Simply demanding compatibility between zvc and best zvn gives 2.5% miss tagging
- Solution: Reject events with a second solution for neutral vertex close to best one
- Require  $|zvn(\text{second}) - zvn(\text{best})| \Delta_{zvn} > xx \text{ cm}$

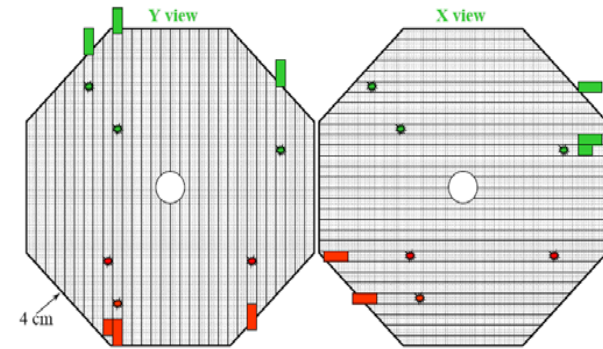


- Evaluation of miss tagging probability with MC. Probability of choosing wrong solution  $< 1.2 \cdot 10^{-3}$  at  $\Delta_{zvn} = 400 \text{ cm}$

# The $K^\pm \rightarrow \pi^\pm \pi^0 \gamma$ decay. Trigger

- L1 trigger
  - Require one track and LKr information (peaks) compatible with at least 3 clusters
  - This introduces an energy dependence  $\rightarrow$  distortion of W distribution
  - **Correction** found using all 3  $\gamma$  events ( $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$  with  $\gamma$  lost) and applied to MC

L1 requires  $n_x > 2$  or  $n_y > 2$



- L2 trigger (rejects  $K^\pm \rightarrow \pi^\pm \pi^0$ )
  - Using DCH information and assuming 60 GeV kaon along z axis on-line processors compute a sort of missing mass of the K- $\pi$  system
  - Cut events compatible with missing mass compatible with  $\pi^0$ . Equivalent to  $T^*_\pi < 90$  MeV cut
  - To keep away of edge resolution effects require  $T^*_\pi < 80$  MeV in analysis



# The $K^\pm \rightarrow \pi^\pm \pi^0 \gamma$ decay. Background

- Most dangerous are  $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$  and  $K^\pm \rightarrow \pi^\pm \pi^0$

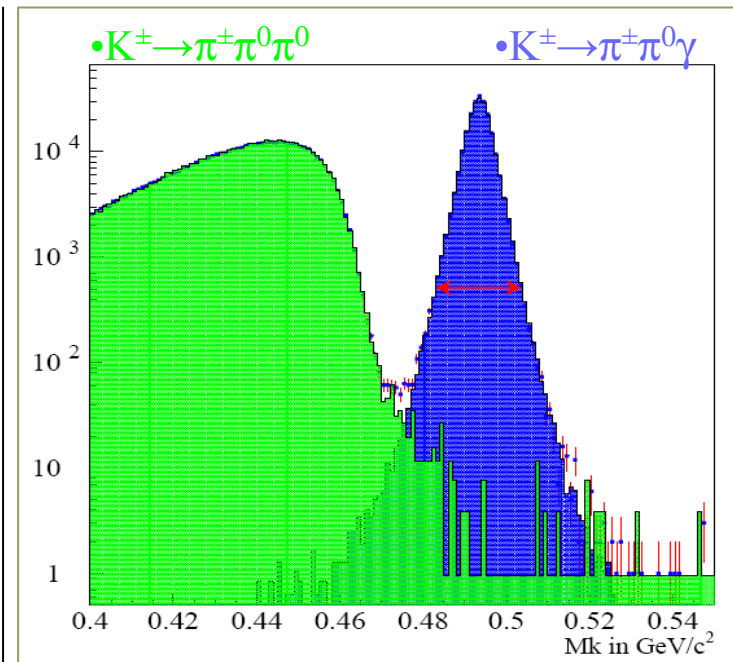
Channel, BR	Mechanism	Cuts
$K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$ ( $1.73 \pm 0.04$ )%	One $\gamma$ lost Overlapping of two $\gamma$	Cog, mass cut ??? Dangerous!!
$K^\pm \rightarrow \pi^\pm \pi^0$ ( $21.13 \pm 0.14$ )%	Accidental clusters Clusters from $\pi$ shower	Time cuts, mass cut Min dist $\pi\gamma$ , mass cut $T_\pi^* < 80$ MeV

- Channels with  $\nu$  easier to reject
  - Smaller BR
  - Mass and cog cuts, particle ID
  - Time cuts for non-radiative

Channel, BR	Channel, BR (cut)
$K^\pm \rightarrow e^\pm \pi^0 \nu$ (Ke3) ( $4.87 \pm 0.06$ )%	$K^\pm \rightarrow e^\pm \pi^0 \nu \gamma$ (Ke3 $\gamma$ ) *( $2.65 \pm 0.20$ ) $10^{-4}$
$K^\pm \rightarrow \mu^\pm \pi^0 \nu$ (K $\mu$ 3) ( $3.27 \pm 0.06$ )%	$K^\pm \rightarrow \mu^\pm \pi^0 \nu \gamma$ (K $\mu$ 3 $\gamma$ ) * $< 6.110^{-5}$

# The $K^\pm \rightarrow \pi^\pm \pi^0 \gamma$ decay. Background

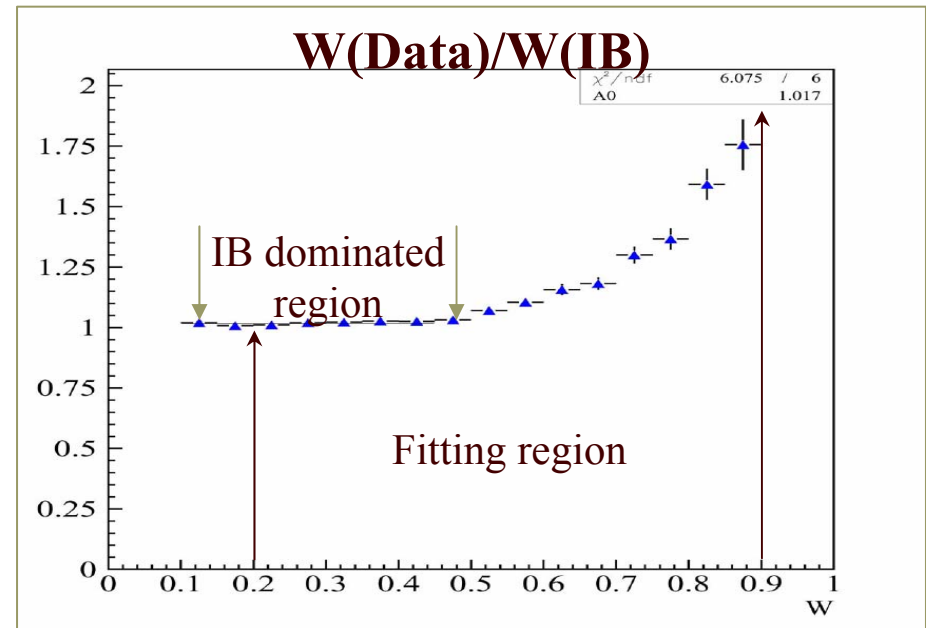
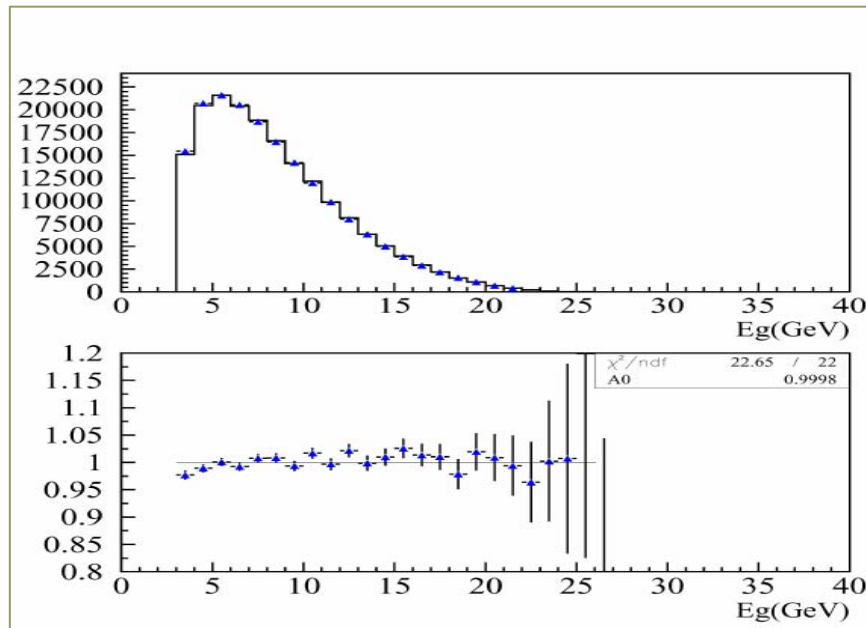
- Cut on overlapping gammas (allows avoiding  $T^*_\pi > 55$  MeV)
  - For every of the 3 gammas in the event assume that its energy  $E_i$  is really the overlap of two gammas of energies  $E_i = x$  and  $E' = (1-x) E_i$
  - Solve for sharing fraction (x) imposing that the two  $\pi^0$  must come from same vertex position. As  $z\pi^0_1 = z\pi^0_2$  solve for x and get  $z\pi^0$
  - Reject event if reconstructed  $z\pi^0$  is compatible with charged z (within 400 cm)
- In addition need to use MUV detector to avoid misreconstruction of track momentum due to  $\pi \rightarrow \mu$  decay in flight
- After cuts the background estimation is  $< 1\%$  of DE



All physical background can be explained in terms of  $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$

# The $K^\pm \rightarrow \pi^\pm \pi^0 \gamma$ decay. Data-MC

- After trigger efficiency correction good agreement MC-Data for  $E_\gamma$ , in particular for  $E_\gamma > 5 \text{ GeV}$  (used for final result)
- $W(\text{Data})/W(\text{MC-IB})$  is in good agreement for IB dominated region and clearly shows DE



# The $K^\pm \rightarrow \pi^\pm \pi^0 \gamma$ decay. Results

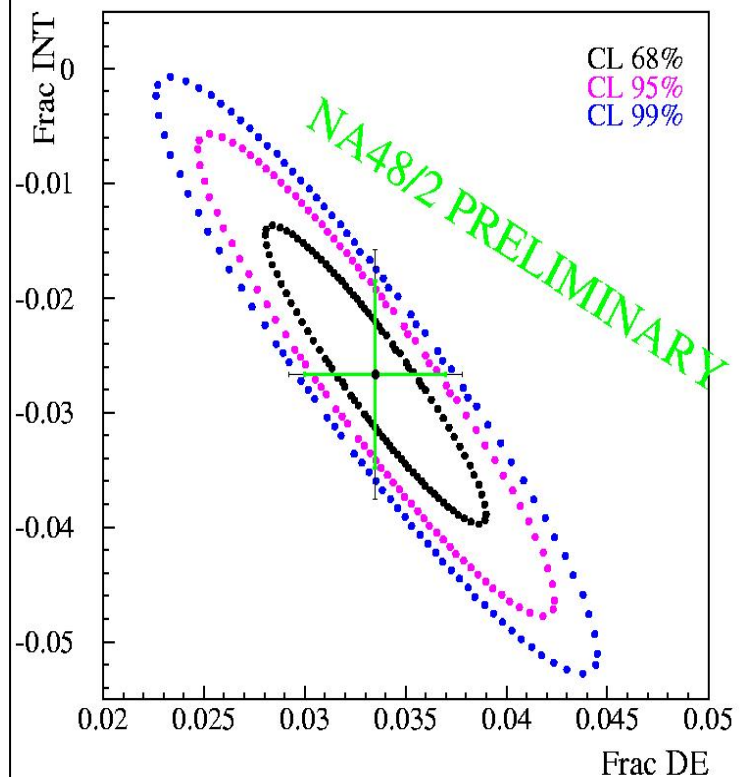
- Use extended ML for  $0.2 < W < 0.9$
- Based on  $124 \cdot 10^3$  events
- Systematic checks:
  - Trigger efficiency dominates (trigger improved for 2004)
  - Neutral energy scale, fitting procedure, miss tagging
- **First evidence of INT!**

**NA48/2 Preliminary: 2003 data**

**$0 < T^*_\pi < 80$  MeV**

$\text{Frac}(\text{DE}) = (3.35 \pm 0.35_{\text{stat}} \pm 0.25_{\text{syst}}) \%$

$\text{Frac}(\text{INT}) = (-2.67 \pm 0.81_{\text{stat}} \pm 0.73_{\text{syst}}) \%$

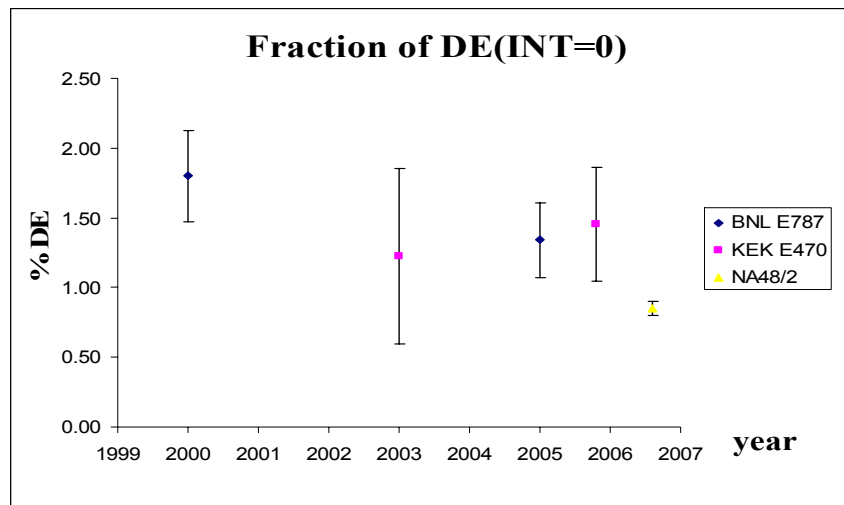


High correlation -0.92

# The $K^\pm \rightarrow \pi^\pm \pi^0 \gamma$ decay. Results

- For comparison: Setting  $\text{INT}=0$ , fitting between  $0 < T_\pi^* < 80$  MeV and extrapolating to  $55 < T_\pi^* < 90$  MeV

$$\text{Frac(DE)} = (0.85 \pm 0.05_{\text{stat}} \pm 0.02_{\text{syst}}) \%$$



# Summary and conclusions

- The branching ratio of  $K_L e3\gamma$  decay has been measured with respect to  $K_L e3$  decay with accuracy. Result in agreement with theory

$$\begin{aligned} & \text{BR}(K_L e3\gamma, E_\gamma^* > 30 \text{ MeV}, \theta_{e\gamma}^* > 20^\circ) / \text{BR}(K_L e3) \\ & = (0.964 \pm 0.008_{\text{stat}} \pm 0.011_{\text{syst}}) \% \end{aligned}$$

- $124 \cdot 10^3$   $K^\pm \rightarrow \pi^\pm \pi^0 \gamma$  events used to extract DE and INT in  $0 < T_\pi^* < 80$  MeV. First evidence for non zero INT term has been found

**NA48/2 Preliminary: 2003 data**

$$\begin{aligned} \text{Frac}(\text{DE}) &= (3.35 \pm 0.35_{\text{stat}} \pm 0.25_{\text{syst}}) \% \\ \text{Frac}(\text{INT}) &= (-2.67 \pm 0.81_{\text{stat}} \pm 0.73_{\text{syst}}) \% \end{aligned}$$



# SPARE

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# ALGORITHM TO REJECT OVERLAPPING GAMMAS

- Overlapping gammas would give right kaon mass.
- For any of the 3 gammas with energies  $E_1, E_2, E_3$  do the following:
- Assume that the gamma with energy  $E_1$  is really the overlap of two gammas of energies  $E=xE_1$  and  $E'=(1-x)E_1$
- Suppose  $E$  comes from a  $\pi^0_1$  together with cluster 2 and  $E'$  was coming from  $\pi^0_2$  with cluster 3. Then the vertices would be:
  - $Z_{\pi^0_1}=(\text{Dist}_{12} * E * E_2)^{1/2} / M_{\pi^0} = (\text{Dist}_{12} * xE_1 * E_2)^{1/2} / M_{\pi^0}$
  - $Z_{\pi^0_2}=(\text{Dist}_{13} * E' * E_3)^{1/2} / M_{\pi^0} = (\text{Dist}_{13} * (1-x)E_1 * E_3)^{1/2} / M_{\pi^0}$
- 3. As  $Z_{\pi^0_1}=Z_{\pi^0_2}$  we can solve for  $x$  and get  $Z_{\pi^0}$
- 4. We reject the event if  $|Z_{\pi^0}-Z_{\text{charged}}| < 500 \text{ cm}$
- Thanks to this cut we can extend region to  $0 < T < 80 \text{ MeV}$  keeping the needed rejection.



# SPARE

Effect	Syst. DE	Syst. INT
Energy scale	+0.09	-0.21
Fitting procedure	0.02	0.19
LVL1 trigger	$\pm 0.17$	$\pm 0.43$
Mistagging	–	$\pm 0.2$
LVL2 Trigger	$\pm 0.17$	$\pm 0.52$
Resolutions difference	$< 0.05$	$< 0.1$
LKr non linearity	$< 0.05$	$< 0.05$
BG contributions	$< 0.05$	$< 0.05$
<b>TOTAL</b>	<b><math>\pm 0.25</math></b>	<b><math>\pm 0.73</math></b>