

Recent results from NA48/2 on  $K_{e4}$  and  $K^{\pm} \rightarrow \pi^{\pm}\pi^0\pi^0$  decays  
Interpretation in terms of  $\pi\pi$  scattering lengths



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On behalf of the NA48/2 collaboration:  
Cambridge, CERN, Chicago, Dubna, Edinburgh, Ferrara, Firenze, Mainz,  
Northwestern, Perugia, Pisa, Saclay, Siegen, Torino, Wien

# Outline

- The NA48/2 experiment : an introduction  
beams, detector and performances
- Ke4 decays in charged ( $K^\pm \rightarrow e^\pm \nu \pi^+ \pi^-$ ) and neutral ( $K^\pm \rightarrow e^\pm \nu \pi^0 \pi^0$ ) :  
modes : variables and Form Factors
- Ke4 results : Form Factors and phase shift in charged decays  
Form Factor and Branching fraction in neutral mode
- K3pi neutral decays ( $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$ ) : the "cusp" effect and Form  
Factors in the Dalitz plot
- Interpretation in terms of  $\pi \pi$  scattering lengths
- Conclusion and prospects

# The NA48/2 experiment: an introduction

The primary goals :

Search for **CP-violating charge asymmetries** ( $K^+ K^-$ ) in  $K^\pm \rightarrow 3 \pi$  decays

Two measurements : "charged"  $\pi^\pm \pi^+ \pi^-$  and "neutral"  $\pi^\pm \pi^0 \pi^0$  asymmetries  
both modes with large **BR's of (2-5)  $10^{-2}$**

( presented by M.Raggi in last week EW session)

but also

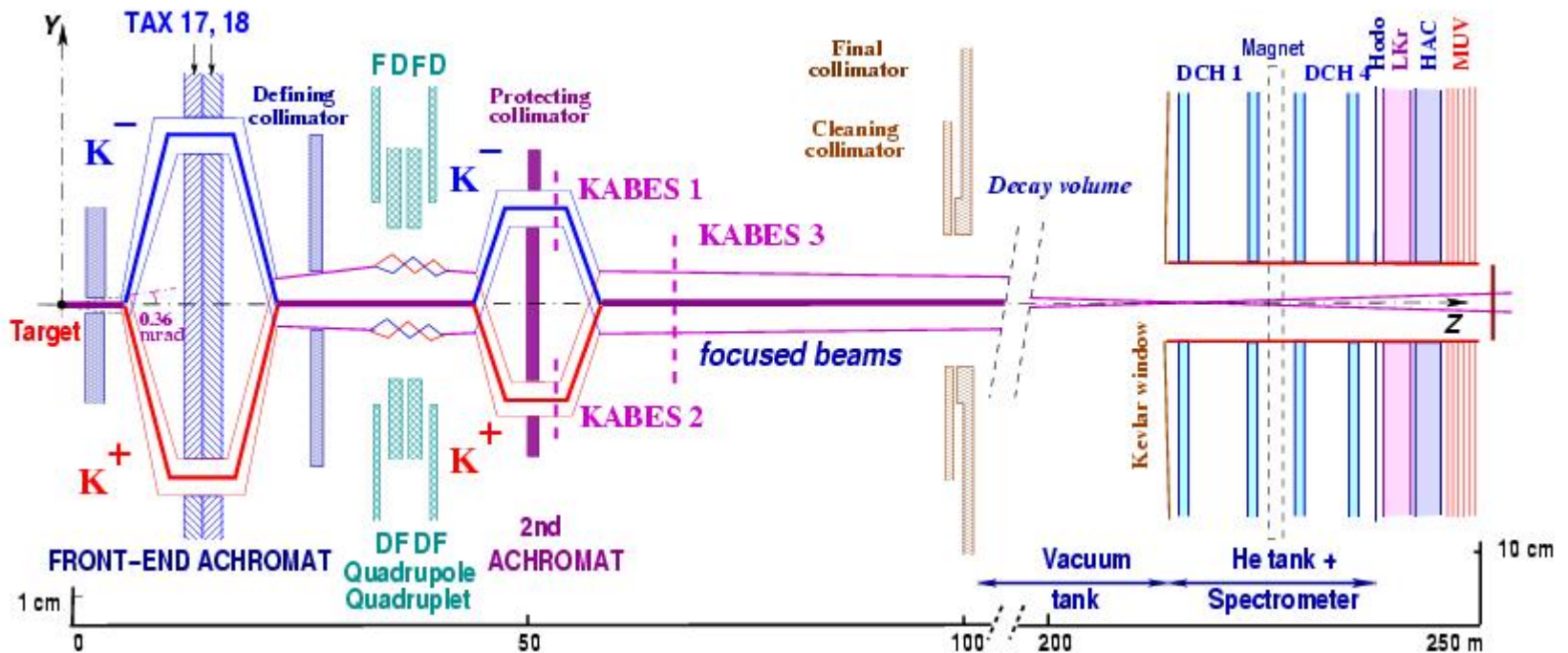
Study of many **rare decays** , in particular **Ke4** in the "charged"  $\pi^+ \pi^- e^\pm \nu$  (and  
"neutral"  $\pi^0 \pi^0 e^\pm \nu$ ) final state, both modes with small **BR's of few  $10^{-5}$**  .

In the  $\pi\pi$  scattering process, it is possible to relate amplitudes with  
different Isospin using dispersion relations (Roy equations) which depend  
essentially on two parameters, the scattering lengths  $a_0^0$  and  $a_0^2$

Chiral PT predictions for low energy  $\pi\pi$  interaction introduce further  
constraints between  $a_0^0$  and  $a_0^2$  which are related to the size of the  
quark condensate.

# The NA48/2 experiment: beams and detector

Simultaneous  $K^+/K^-$  beams :  $(60 \pm 3) \text{ GeV}/c$



2003 Run ~50 days

2004 Run ~60 days

# The NA48/2 experiment: detector performances

Most important components for  $K_{e4}/K_{3\pi}$  analysis :

**Magnetic spectrometer** : 4 high-resolution DCH's

$$\Delta p/p = (1.0 \oplus 0.044 p)\% \quad (p \text{ in } \text{GeV}/c)$$

→ Very good resolution for **charged invariant masses** (Kaon)

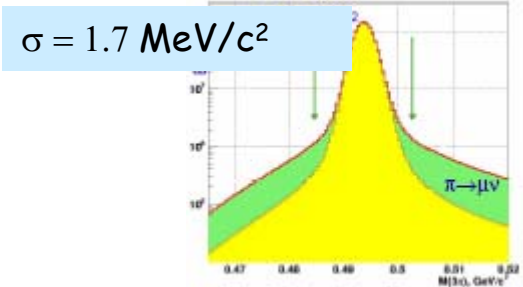
**LKr electromagnetic calorimeter** : quasi-homogenous and high granularity

$$\Delta E/E = (3.2/\sqrt{E} \oplus 9.0/E \oplus 0.42)\% \quad (E \text{ in } \text{GeV})$$

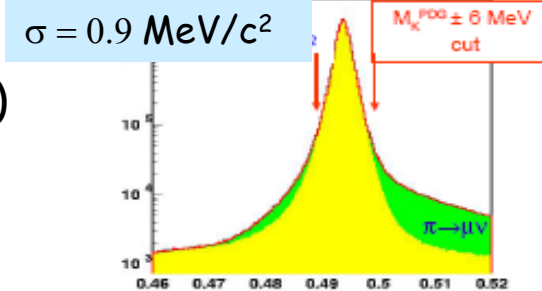
$$\sigma_x = \sigma_y \sim 1.5 \text{ mm for } E=10 \text{ GeV}$$

→ Very good resolution for **neutral invariant masses** ( $\pi^0$ )

→ E/p ratio for **e/ $\pi$  discrimination**



$(\pi^\pm \pi^+\pi^-)$  mass  $\text{GeV}/c^2$



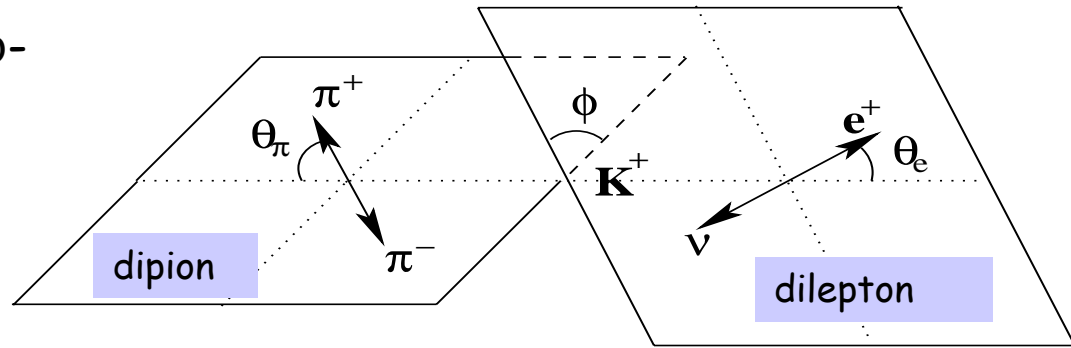
$(\pi^\pm \pi^0\pi^0)$  mass  $\text{GeV}/c^2$

# Ke4 charged decays : formalism

Five kinematic variables ( Cabibbo-Maksymowicz):

$$S_\pi (M_{\pi\pi}^2), S_e (M_{e\nu}^2),$$

$$\cos\theta_\pi, \cos\theta_e \text{ and } \phi.$$



partial wave expansion of the amplitude:

$F, G =$  Axial Form Factors

$$F = F_s e^{i\delta_s} + F_p e^{i\delta_p} \cos\theta_\pi + \text{d-wave term...}$$

$$G = G_p e^{i\delta_g} + \text{d-wave term...}$$

$H =$  Vector Form Factor

$$H = H_p e^{i\delta_h} + \text{d-wave term...}$$

expansion in powers of  $q^2$ ,  $S_e$

$$(q^2 = (S_\pi / 4m_\pi^2 - 1))$$

$$F_s = f_s + f'_s q^2 + f''_s q^4 + f_e (S_e / 4m_\pi^2) + ..$$

$$F_p = f_p + f'_p q^2 + ..$$

$$G_p = g_p + g'_p q^2 + ..$$

$$H_p = h_p + h'_p q^2 + ..$$

The fit parameters are :  $F_s$   $F_p$   $G_p$   $H_p$  and  $\delta = \delta_s - \delta_p$

# Ke4 decays: event selection and background rejection

**Signal** ( $\pi^+\pi^-e^\pm\nu$ ) **Topology** : 3 charged tracks , two opposite sign pions, 1 electron (LKr info E/p), some missing energy and  $p_T$  (neutrino)

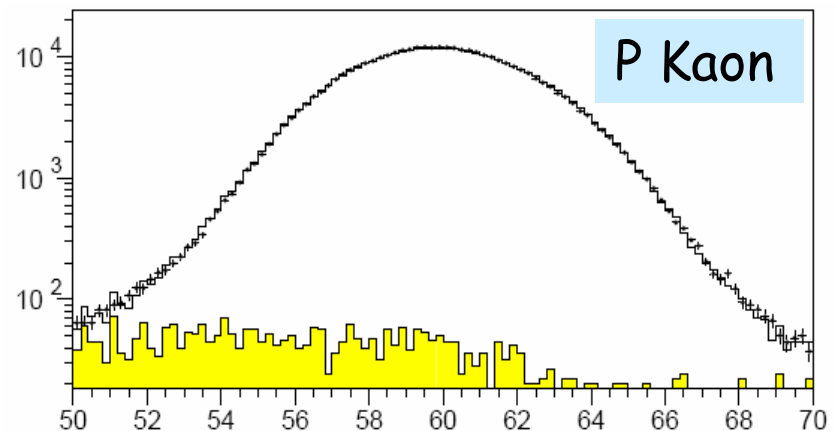
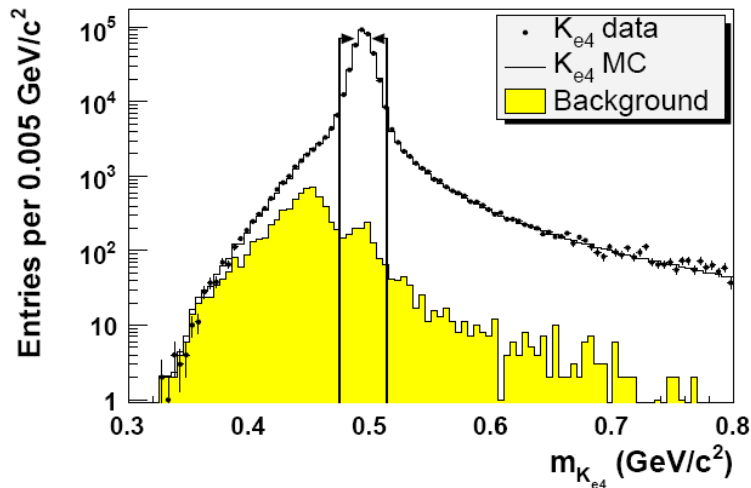
**Background** : main sources

$\pi^\pm \pi^+ \pi^-$  decay +  $\pi \rightarrow e \nu$  decay (dominant) or +  $\pi$  misidentified as e

$\pi^\pm \pi^0(\pi^0)$  decay +  $\pi^0$  Dalitz decay ( $e^+e^-\gamma$ ) + e misidentified as  $\pi$  and  $\gamma$  (s) undetected

**Control from data sample** : **Wrong Sign** events have the same total charge but  $e^-$  and  $\pi^+ \pi^+$  for  $K^+$  decays ( $e^+$  and  $\pi^- \pi^-$  for  $K^-$  decays). Depending on the process, background events appear in **Right Sign** events with the **same rate** or **twice the rate** of the WS events

**Total background level** can be kept at  $\sim 0.5\%$  relative level



## Ke4 charged decays : Form Factor determination

Using **iso-populated bins** in the 5-dimension space of the C.M. variables, ( $M_{\pi\pi}$ ,  $M_{e\nu}$ ,  $\cos\theta_{\pi}$ ,  $\cos\theta_e$  and  $\phi$ ) one defines a grid of

**10x5x5x5x12=15000 boxes.**

The set of Form Factor values is used to minimize a log-likelihood estimator well suited for small numbers of **data events/bin** and taking into account the statistics of the simulation (**simulated** and **expected events/bin**).

K <sup>+</sup> sample (235000 events)	16 events/box
K <sup>-</sup> sample (135000 events)	9 events/box
MC K <sup>+</sup> sample (5.5 Millions events)	~370 events/box
MC K <sup>-</sup> sample (3.0 Millions events)	~200 events/box

Ratio **K<sup>+</sup>/K<sup>-</sup> ~ 1.8** both in Data and MC (run by run basis)

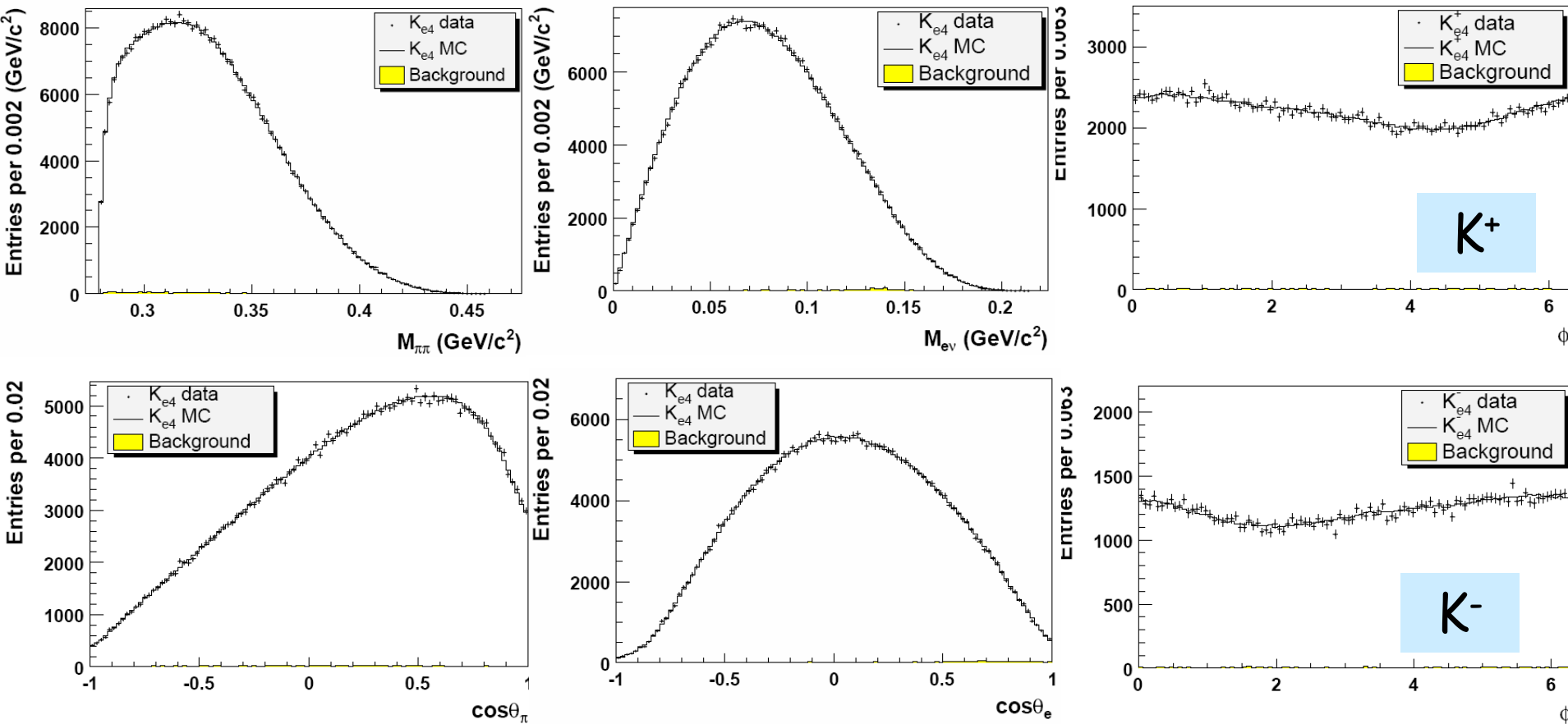
Ratio **MC/Data ~ 23.** both for K<sup>+</sup> and K<sup>-</sup> (run by run basis)



# Ke4 charged decays : the 5 distributions

CP symmetry :  $(K^+)_{\phi}$  distribution is opposite of  $(K^-)_{\phi}$  distribution

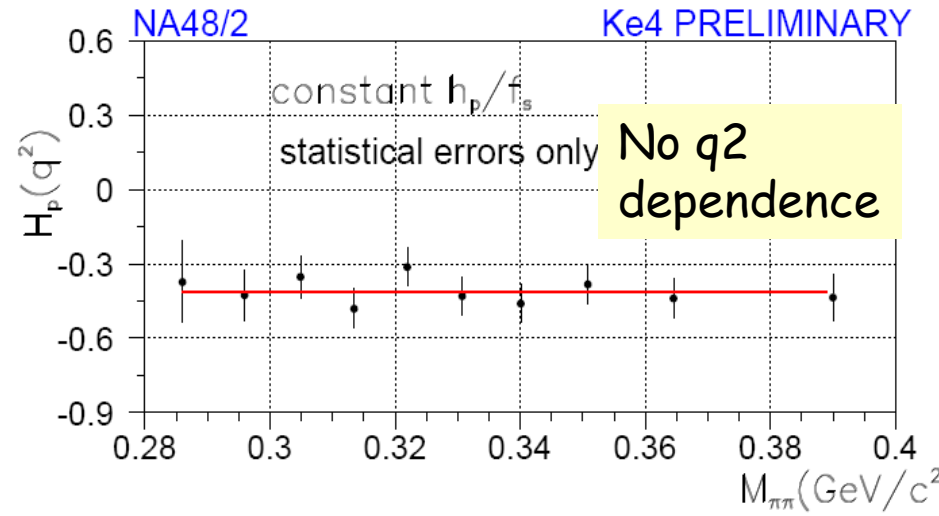
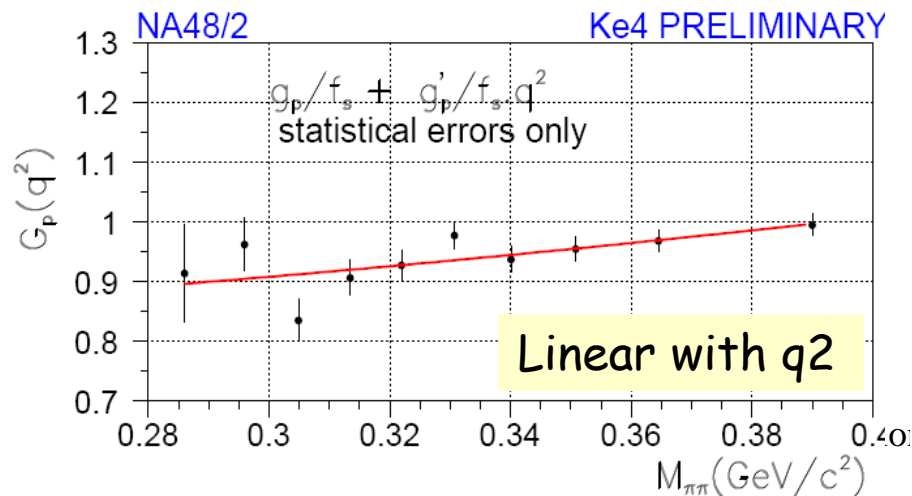
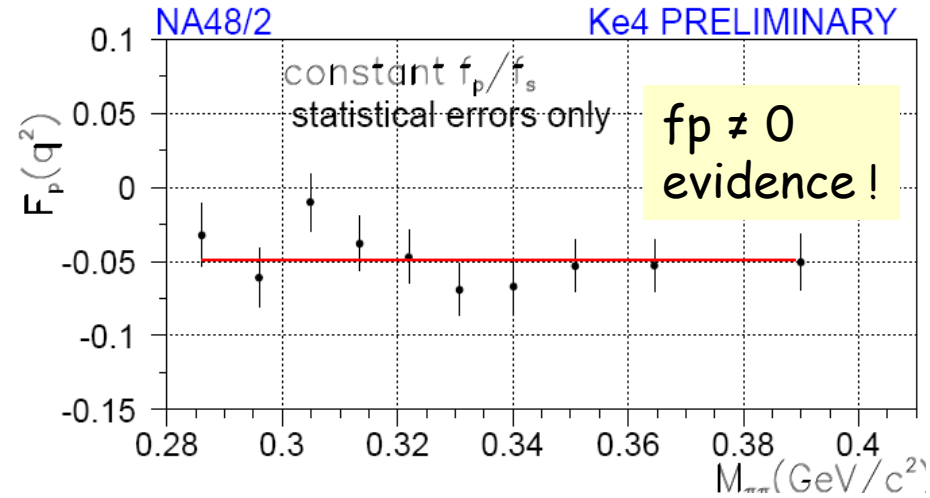
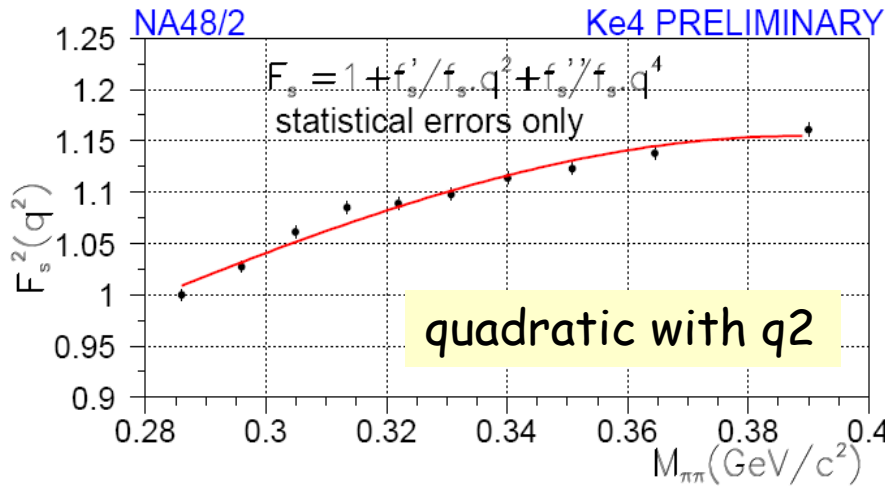
$K^+$  and  $K^-$  samples fitted separately, results combined



# Ke4 charged decays : F,G,H form factors

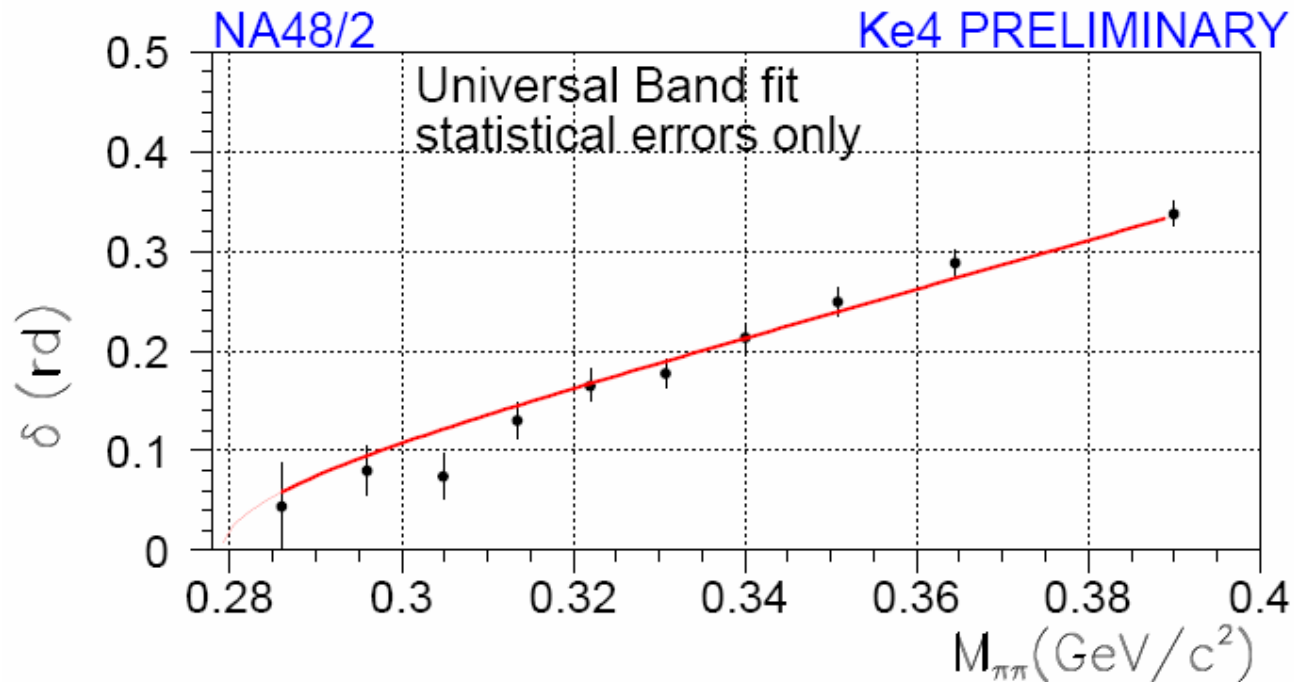
Ten independent fits, one in each  $M_{\pi\pi}$  bin, assuming  $\sim$ constant form factors over each box. This allows a model independent analysis.

Without the overall normalization (Branching fraction), one can quote relative form factors and their variations with  $q^2, q^4$  ( $q^2 = (S_{\pi}/4m_{\pi}^2 - 1)$ )



## Ke4 charged decays : $\delta$ form factor and $a_0^0$

To extract information from the  $\delta = (\delta_0^0 - \delta_1^1)$  variation, some external data ( $I=2 \pi\pi$  data @Higher energy) and theoretical work are needed : the numerical solution of Roy equations (ACGL Phys. Rep.353 (2001), DFGS EPJ C24 (2002) ) relates  $\delta$  and  $(a_0^0, a_0^2)$ . The **Universal Band** parameterization corresponds to a 1-parameter fit with  $a_0^2 = f(a_0^0)$ .



# Ke4 charged decays : preliminary results (370 000 decays)

## Snapshot on systematics :

- Two independent analyses with slightly different **approaches** ( binning, trigger efficiency, fit method..)
- **Acceptance** control
- **Background level** and **shape** control :
- **Electron identification** control
- **Radiative corrections** implementation
- **Neglected  $S_e$  dependence**

## Form Factors $K^+$ and $K^-$ combined

$$f'_s / f_s = \mathbf{0.169 \pm 0.009 \pm 0.034}$$

$$f''_s / f_s = \mathbf{-0.091 \pm 0.009 \pm 0.031}$$

$$f_p / f_s = \mathbf{-0.047 \pm 0.006 \pm 0.008}$$

$$g_p / f_s = \mathbf{0.891 \pm 0.019 \pm 0.020}$$

$$g'_p / f_s = \mathbf{0.111 \pm 0.031 \pm 0.032}$$

$$h_p / f_s = \mathbf{-0.411 \pm 0.027 \pm 0.038}$$

$$a_0^0 = \mathbf{0.256 \pm 0.008 \pm 0.007}$$

$\pm 0.018$  Theory (Universal Band)

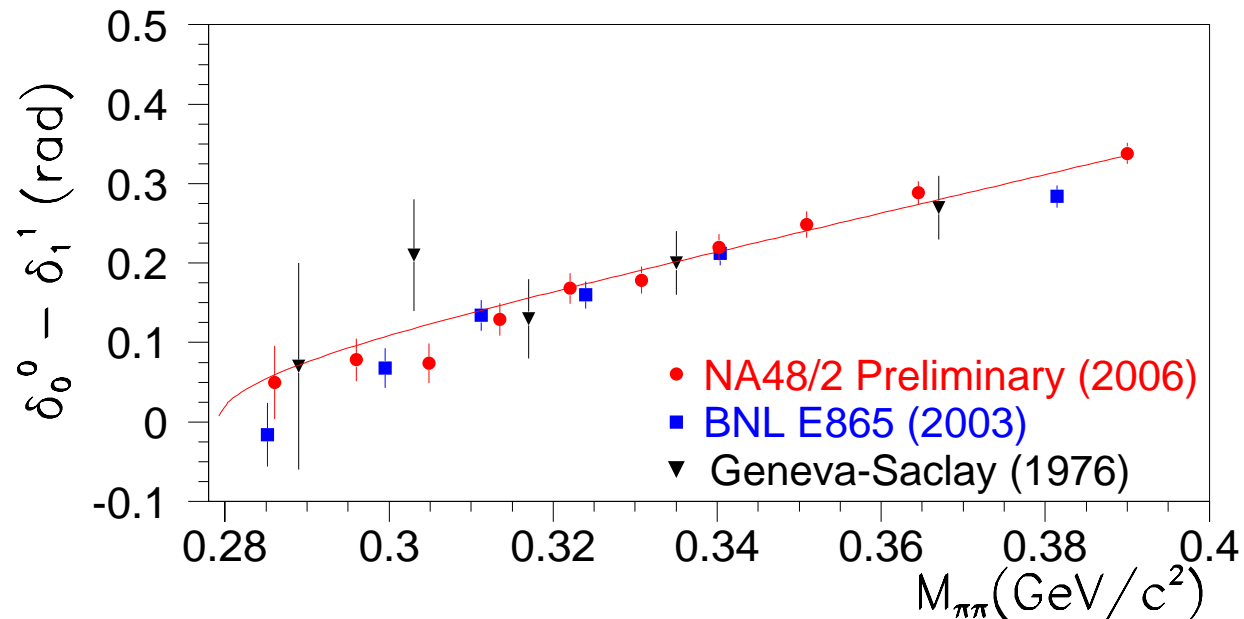
Corresponding to  $a_0^2 = \mathbf{-0.031 \pm 0.002 \pm 0.002}$   
 $\pm 0.009$  Theory ( full UB width)

## Ke4 charged decays : towards $\pi\pi$ scattering lengths

Comparison with previous published Ke4 results :

- CERN/PS Geneva-Saclay  $\sim 30000$  decays ( $K^+$ ) (Phys. Rev. D15 (1977))
- BNL E865  $\sim 390\,000$  decays ( $K^+$ ) (PRL 87 (2001), Phys. Rev. D67 (2003))
- CERN/SPS NA48/2 : prelim. result from  $\sim 370\,000$  decays ( $K^+/K^-$ )  
significant acceptance at larger  $m_{\pi\pi}$  values, high resolution and low background level.

Universal Band centre line shown (stat. + experimental syst. errors added)



# Ke4 neutral decays : Branching fraction

**Signal**  $\pi^0 \pi^0 e^\pm \nu$  **Topology** : 1 charged track , 2  $\pi^0$ 's (reconstructed from 4 $\gamma$ 's in LKr), 1 electron (LKr info E/p), some missing energy and  $p_T$  (neutrino)

2003 data : ~10000 signal events (with ~3% background events)

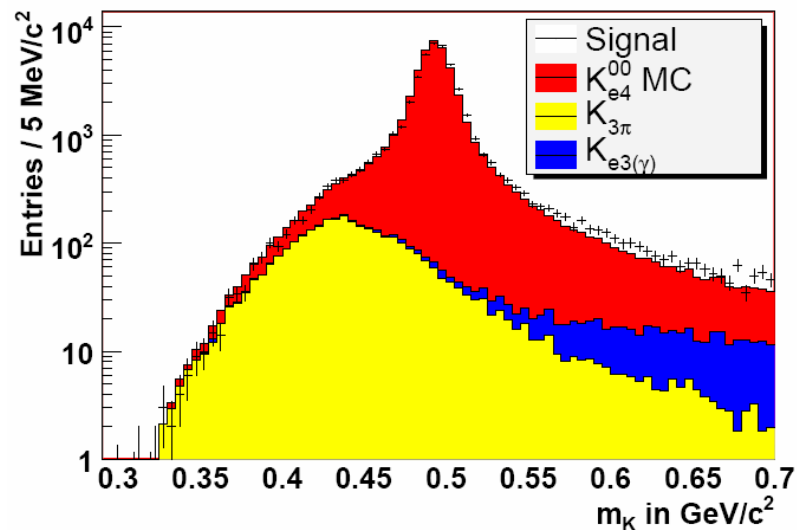
2004 data : ~30000 signal events (with ~2% background events)

**Background** : main sources estimated from data by reverting cuts

$\pi^\pm \pi^0 \pi^0$  decay +  $\pi$  misidentified as  $e$  (dominant)

$\pi^0 e^\pm \nu \gamma$  decay + accidental  $\gamma$

Systematics from acceptance, trigger, electron id



Branching fraction (2003 data,  $K^+$  and  $K^-$ ) using  $(\pi^\pm \pi^0 \pi^0)$  as normalization

$$\text{Br}(\text{Ke4 neutral}) = (2.587 \pm 0.026 \text{ stat} \pm 0.019 \text{ syst} \pm 0.029 \text{ ext}) 10^{-5}$$

10 times more precise than previous measurement :

KEK E470 based on 216 signal events

$$(2.29 \pm 0.33) 10^{-5}$$

# Ke4 neutral decays : Form Factor

(two identical  $\pi^0 \rightarrow$  only **ONE** Form Factor  $F_s$ , no p-wave !)

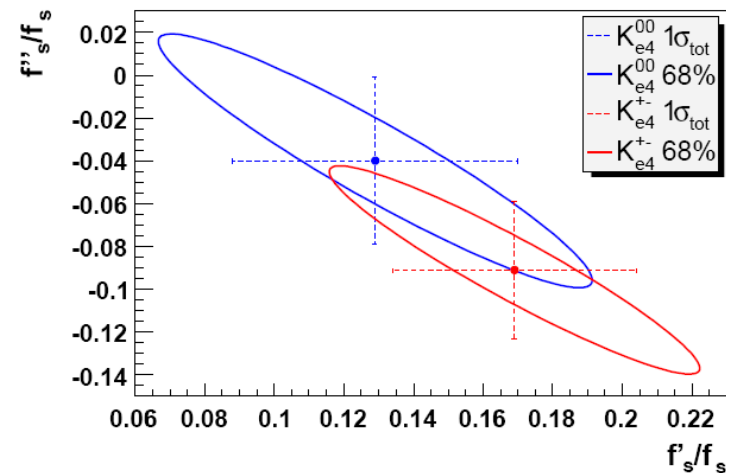
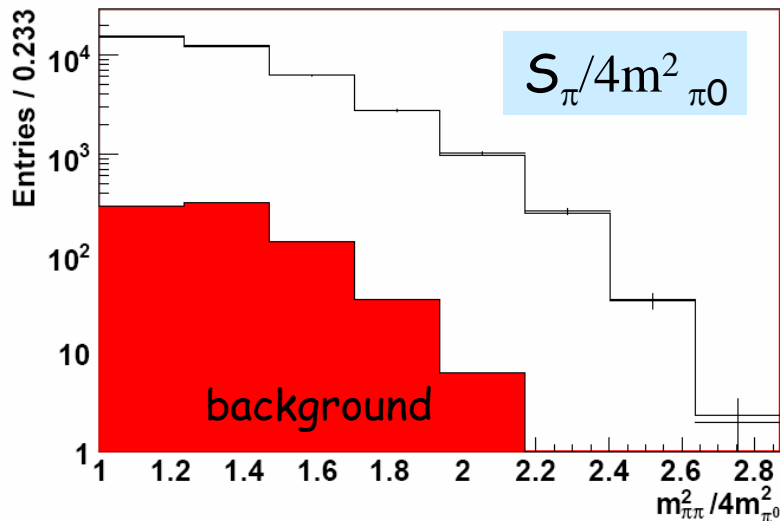
$$F_s = f_s + f'_s q^2 + f''_s q^4 + f_e \left( S_e / 4m_\pi^2 \right) + ..$$

Form factors (2003 +2004 data,  $K^+$  and  $K^-$ )

$S_e$  dependence measurement consistent with 0.

$$f'_s / f_s = 0.129 \pm 0.036_{stat} \pm 0.020_{syst}$$

$$f''_s / f_s = -0.040 \pm 0.034_{stat} \pm 0.020_{syst}$$

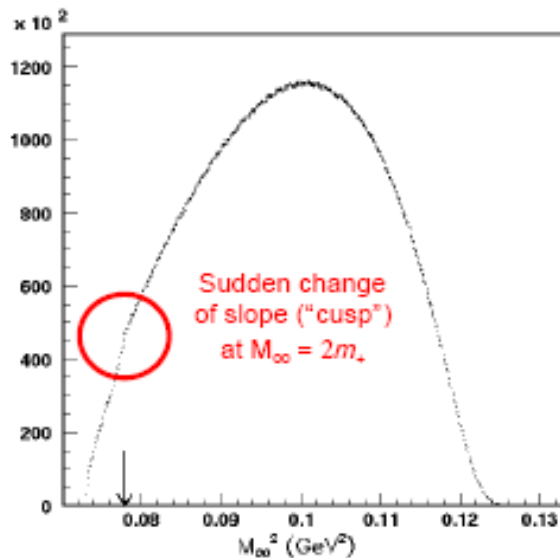


Ke4 charged and neutral FF consistent

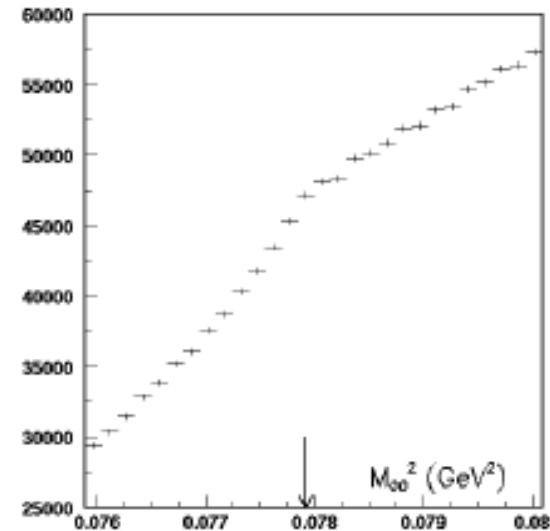
# The cusp effect in $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$ decays

Result published in Phys. Lett. B633 (2006)

Reminder: from  $23 \times 10^6$  ( $\pi^\pm \pi^0 \pi^0$ ) decays, the  $M_{00}^2$  shows a sudden change of slope at  $M_{00} = 2m_{\pi^\pm}$



"Zoom" on the cusp region

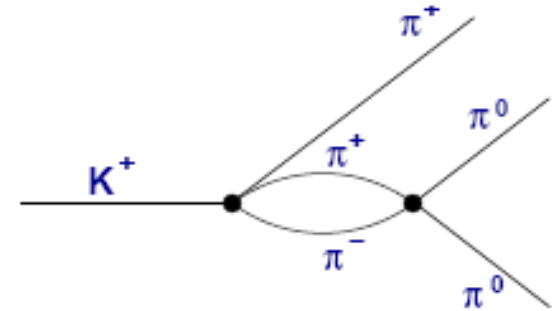




# The cusp effect : fit method and results

**Principle:** 1-dimension fit to the  $M_{00}^2$  distribution based on the improved rescattering model of Cabibbo-Isidori (JHEP 0503 (2005))

In the Dalitz plot,  $g_0$  and  $h'$  are free parameters while **parameter  $k$  is set to 0.**



$$M_0 = A_0 \left( 1 + \frac{1}{2} g_0 u + \frac{1}{2} h' u^2 + \frac{1}{2} k v^2 \right)$$

Form Factors as in Phys.Lett.B633(2006)

$$g_0 = 0.645 \pm 0.004_{\text{stat}} \pm 0.009_{\text{syst}}$$

$$h' = -0.047 \pm 0.012_{\text{stat}} \pm 0.011_{\text{syst}}$$

$$a_2 = -0.041 \pm 0.022_{\text{stat}} \pm 0.014_{\text{syst}}$$

$$(a_0 - a_2) = 0.268 \pm 0.010_{\text{stat}} \pm 0.004_{\text{syst}} \pm 0.013_{\text{ext}}$$

Correlation

$$\rho(a_0 - a_2, a_2) = -0.858$$

if the  $a_2$  value predicted/preferred by ChPT is fixed,

$$(a_0 - a_2) = 0.264 \pm 0.006_{\text{stat}} \pm 0.004_{\text{syst}} \pm 0.013_{\text{ext}}$$

# The cusp effect : more investigations for a k term

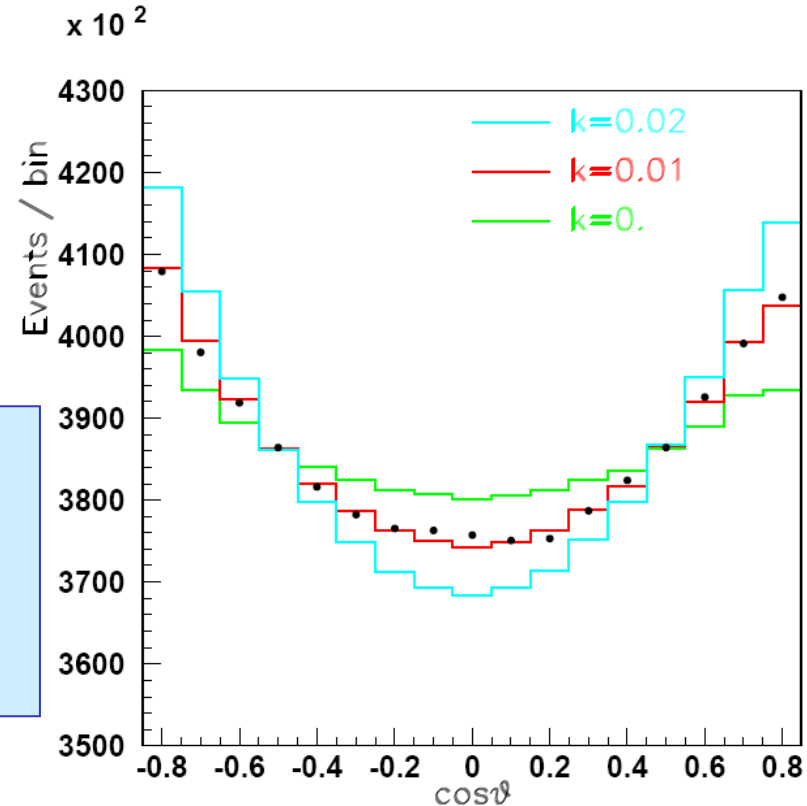
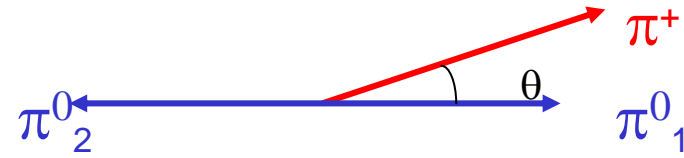
Going to a 2D fit would imply to use  $(M_{00}^2, M_{+0}^2)$  variables. An alternate choice is  $(M_{00}^2, \cos\theta)$  where  $\theta$  is the angle between the charged  $\pi$  and the direction of the  $\pi^0$ 's in their rest frame.

Use a modified matrix element :

$$M_0 = A_0 \left( 1 + \frac{1}{2} g_0 u + \frac{1}{2} h' u^2 + \frac{1}{2} k' v^2 \right)$$

re-fit in  $M_{00}^2$  range  $[0.082, 0.097] (\text{GeV}/c^2)^2$

no incidence on previous  $(a_0 - a_2)$  result.



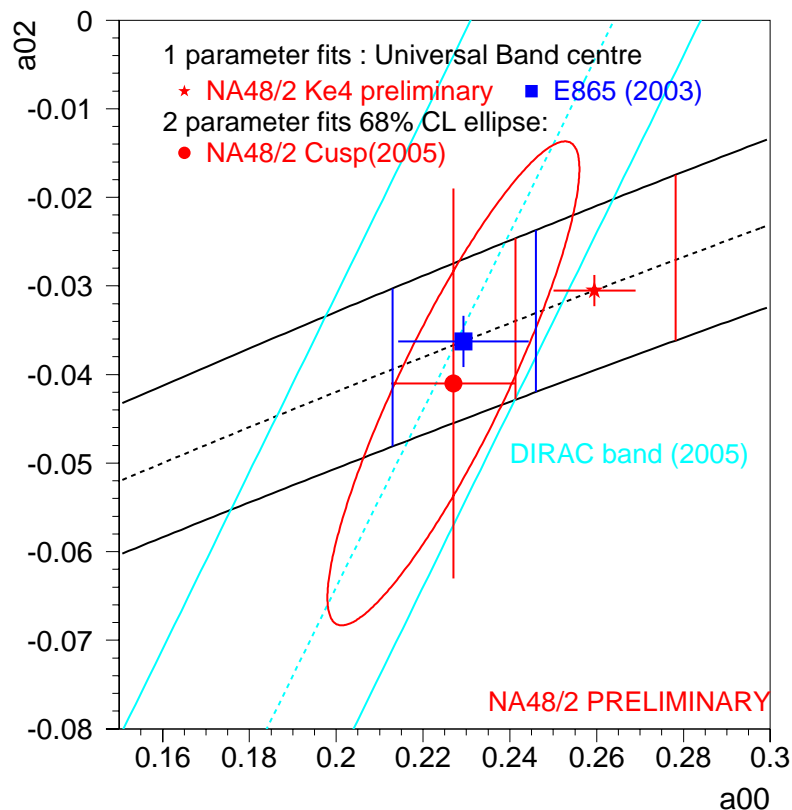
Preliminary result (2003 data,  $K^+$  and  $K^-$ )

$$k' = 0.0097 \pm 0.0003_{\text{stat}} \pm 0.0008_{\text{syst}}$$

Note: the different meaning  $(g_0, h', k')$  wrt PDG  $(g_0, h, k)$

# $\pi\text{-}\pi$ scattering lengths in NA48/2 : Summary and prospects

NA48/2 uses 2 independent channels to access  $\pi\text{-}\pi$  scattering lengths: phase shift from the Ke4 decays and the cusp effect in  $\pi^\pm \pi^0 \pi^0$  decays.



Other measurements (E865 Ke4, DIRAC pionium  $\tau$ ) also available

They **maybe** compared BUT **beware of (implicit) theoretical frameworks!**

Future Improvements from NA48 in a few months (KAON 07 in May)

Cusp : 70 M events (2003+2004) + improved theory input

Ke4 : ~0.65 M events (2003) + more elaborated theory input

# Conclusions

Ke4

Using partial data samples recorded in 2003-2004, Na48/2 has improved measurements of the **Ke4 form factors** in the charged and neutral modes (5 to 30% stat. precision). **Non zero fp term observed**

$$\text{BR}(\text{Ke4}^{00}) = (2.587 \pm 0.026_{\text{stat}} \pm 0.019_{\text{syst}} \pm 0.029_{\text{theo}}) \cdot 10^{-5}$$

(10 times better than current PDG value)

Using a conservative theoretical approach, a **preliminary** value of  $a_0^0$  is obtained with **3% precision (both stat. and syst.)**. More constrained result in progress with help from theorists.

$$a_0^0 = 0.256 \pm 0.008_{\text{stat}} \pm 0.007_{\text{syst}} \pm 0.018_{\text{theo}} \quad (\text{Universal Band width})$$

New measurements of Matrix element and  $\pi\pi$  scattering length in K3pi decays

$$a_0^0 - a_0^2 = 0.268 \pm 0.010_{\text{stat}} \pm 0.004_{\text{syst}} \pm 0.013_{\text{theo}}$$

First evidence for a non-zero  $k'$  term

$$k' = 0.0097 \pm 0.0003_{\text{stat}} \pm 0.0008_{\text{syst}}$$

Cusp

More stringent constrains in the  $(a_0^0, a_0^2)$  plane to be expected soon