

## NEW RESULTS ON KAON DECAYS FROM NA48/2

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Recent results from the NA48/2 experiment are presented. The  $\pi\pi$  scattering lengths  $a_0^0$  and  $a_0^2$  have been extracted from the cusp in the  $M_{00}^2$  distribution of  $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$  decays and from the  $K^\pm \rightarrow \pi^+ \pi^- e^\pm \nu$  phase shift  $\delta$ . Branching ratios and form factors have been measured for  $K^\pm \rightarrow \pi^\pm \gamma \gamma$ ,  $K^\pm \rightarrow \pi^\pm \gamma e^+ e^-$  and  $K^\pm \rightarrow \pi^\pm e^+ e^-$  decays and are also summarized here.

### 1 Introduction

During 2003 and 2004, the NA48/2 experiment at CERN SPS has collected the world largest amount of charged kaon decays. The main goal of NA48/2 was the search for direct CP violation in  $K^\pm$  decays into three pions. However, given the high statistics achieved, many other physics topics were also covered including the study of the  $\pi\pi$  interaction at low energy, radiative decays, the measurement of  $V_{us}$  from semileptonic decays, etc.. In the following sections, recent results on ChPT parameters obtained by the NA48/2 Collaboration will be presented.

### 2 The NA48/2 experiment

Simultaneous  $K^+$  and  $K^-$  beams were produced by 400 GeV protons from the CERN SPS, impinging on a Be target. Kaons were deflected in a front-end achromat to select a momentum band of  $60 \pm 3$  GeV/ $c$  and then focused such that they converge about 200 m downstream at the beginning of the detector. A description of the detector can be found in <sup>1</sup>. For the measurements presented here, the most important detector components are the magnet spectrometer, consisting of two drift chambers before and two after a dipole magnet, and the quasi-homogeneous liquid krypton calorimeter. The momentum of the charged particles and the energy of the photons are measured with a relative uncertainty of 1% at 20 GeV. The trigger was mainly designed to select events with three charged tracks (charged trigger) and  $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$  events (neutral trigger).

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<sup>a</sup>On behalf of the NA48/2 Collaboration.

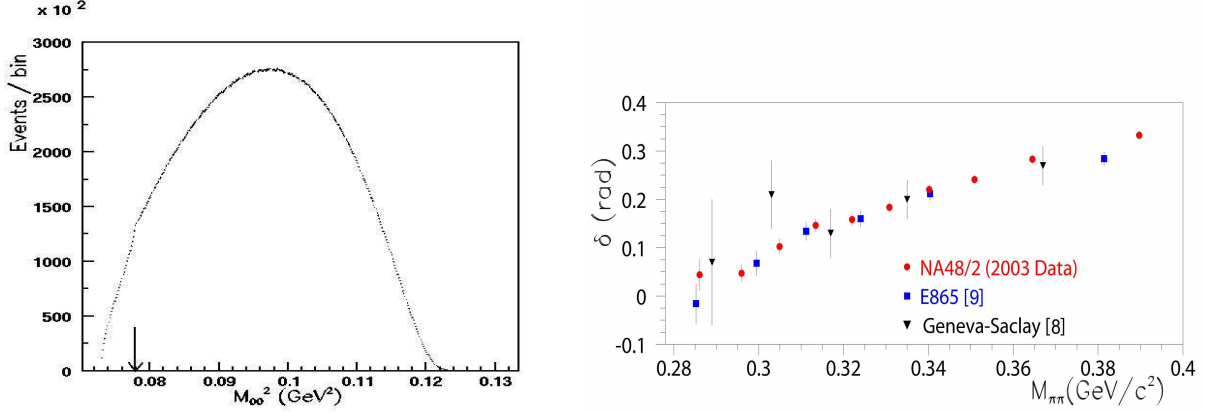


Figure 1: (Left) Invariant  $\pi^0\pi^0$  mass squared of  $K^\pm \rightarrow \pi^\pm\pi^0\pi^0$  candidates. Note the presence of a cusp for  $M_{00}^2 = 4m_{\pi^+}^2$  (arrow). (Right) Variation of phase shift in  $K^\pm \rightarrow \pi^+\pi^-e^\pm\nu$  decays with  $\pi^+\pi^-$  invariant mass.

### 3 Measurement of $\pi\pi$ scattering lengths

The quark condensate  $\langle 0|\bar{q}q|0\rangle$  is a fundamental parameter of ChPT. Its value must be determined experimentally, e.g. by measuring the  $\pi\pi$  scattering lengths  $a_0^0$  and  $a_0^2$ , which are predicted very precisely within the framework of ChPT<sup>2</sup>.

NA48/2 has reported two new measurements of the  $\pi\pi$  scattering lengths using  $K^\pm \rightarrow \pi^\pm\pi^0\pi^0$  and  $K^\pm \rightarrow \pi^+\pi^-e^\pm\nu$  decays. A cusp observed in the  $M_{\pi^0\pi^0}$  distribution of  $K^\pm \rightarrow \pi^\pm\pi^0\pi^0$  decays at  $M_{00}^2 = 4m_{\pi^\pm}^2$  (Fig. 1 (left)) can be explained by  $\pi^+\pi^-$  re-scattering terms<sup>3,4</sup> and provides a measurement of  $a_0^0$  and  $a_0^2$  from a fit of the  $M_{00}^2$  distribution around the cusp discontinuity. A sample of about  $59.6 \times 10^6$  decays from 2003 and 2004 data has been used for this analysis, and the preliminary results from the fit of the Cabibbo-Isidori model<sup>5</sup> are:

$$\begin{aligned} (a_0^0 - a_0^2)m_{\pi^+} &= 0.261 \pm 0.006_{stat} \pm 0.003_{syst} \pm 0.001_{ext} \pm 0.013_{theory}, \\ a_0^2 m_{\pi^+} &= -0.037 \pm 0.013_{stat} \pm 0.009_{syst} \pm 0.002_{ext}, \end{aligned} \quad (1)$$

where the theoretical uncertainty is due to neglected  $O(a_i^3)$  and radiative corrections. Alternative fits are being performed following the approach by<sup>6</sup>.

In  $K^\pm \rightarrow \pi^+\pi^-e^\pm\nu$  decays, the pions are produced close to threshold. The decay amplitude depends on the complex phases  $\delta_0$  and  $\delta_1$  (the  $S$  and  $P$  waves  $\pi\pi$  phase shifts for isospin  $I = 0$ ). The difference  $\delta = \delta_0 - \delta_1$  can be measured as a function of the invariant mass of the two pions,  $M_{\pi\pi}$ . NA48/2 has performed a combined fit to the decay form factors and the phase shift difference as a function of  $M_{\pi\pi}$  in a sample of 670000 signal candidates with 0.5% background<sup>7</sup>. The results are shown in Fig. 1 (right) together with two earlier experiments<sup>8,9</sup>. From the phase shift measurements, the  $\pi\pi$  scattering lengths can be extracted using dispersion relations<sup>10</sup>. At the center of the Universal Band<sup>11</sup>,  $a_0^2$  is related to  $a_0^0$ . A one parameter fit gives  $a_0^0 = 0.256 \pm 0.006_{stat} \pm 0.002_{syst} \pm 0.018_{ext}$ , which implies  $a_0^2 = -0.0312 \pm 0.0011_{stat} \pm 0.0004_{syst} \pm 0.0122_{ext}$ . The external error reflects the width of the Universal Band. From a two parameters fit, the results are:

$$\begin{aligned} a_0^0 m_{\pi^+} &= 0.233 \pm 0.016_{stat} \pm 0.007_{syst}, \\ a_0^2 m_{\pi^+} &= -0.047 \pm 0.011_{stat} \pm 0.004_{syst}, \end{aligned} \quad (2)$$

with  $\rho = 0.967$ . Theoretical work including isospin symmetry breaking effects<sup>12</sup> suggests that  $a_0^0$  could decrease by  $\approx 0.02$  for and  $a_0^2$  by  $\approx 0.004$ , bringing this measurement in agreement with other measurements and ChPT predictions<sup>7</sup>.

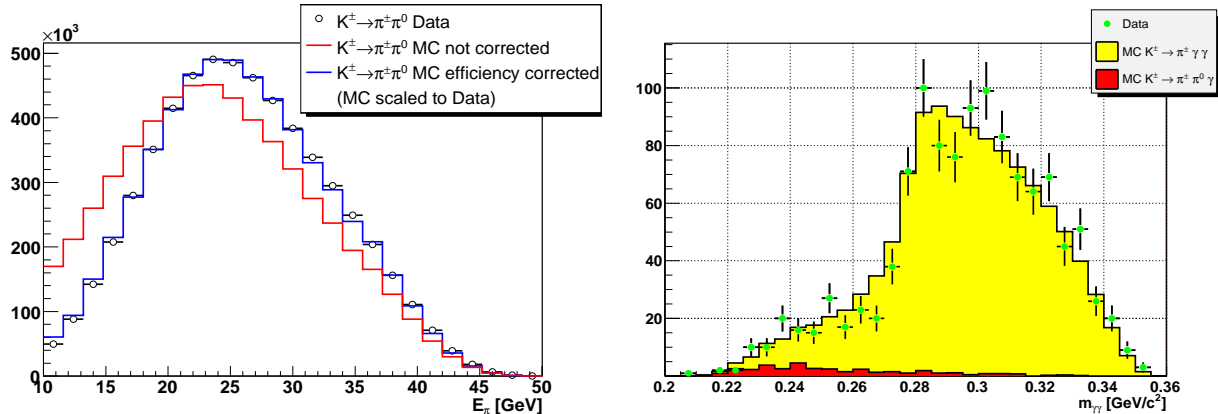


Figure 2: (Left) Pion track energy of  $K^\pm \rightarrow \pi^\pm \pi^0$  normalization data (black) and MC events (red, blue) without and with trigger efficiency correction, respectively. (Right)  $M_{\gamma\gamma}$  invariant mass of  $K^\pm \rightarrow \pi^\pm \gamma\gamma$  candidates.

#### 4 $K^\pm \rightarrow \pi^\pm \gamma\gamma$ analysis

The contributions of the chiral lagrangian to this decay<sup>13</sup> appear at  $O(p^4)$ . At this order, only the  $\Delta I = 1/2$  invariant amplitudes  $A(z)$  and  $C(z)$  with  $z = M_{\gamma\gamma}^2/M_{K^\pm}^2$  contribute.  $A(z)$  contains the  $O(p^4)$  *loop diagram* contributions and the *tree level counterterms* absorbed in unknown parameter  $\hat{c}$  predicted to be positive and of  $O(1)$ <sup>14</sup>. The loop leads to a characteristic signature in the invariant mass  $M_{\gamma\gamma}$  distribution, which is favoured to be above  $2m_{\pi^+}$  and exhibits a cusp at  $2m_{\pi^+}$  threshold. The parameter  $\hat{c}$  fixes the value of the branching ratio and the  $M_{\gamma\gamma}$  spectrum shape.  $C(z)$  contains *poles and tadpoles*<sup>13,15</sup> effects.  $O(p^6)$  studies concluded<sup>16</sup> that unitarity correction effects could increase the BR between 30% – 40%, while vector meson exchange contributions would be negligible.

NA48/2 has analyzed about 40% of its data, finding 1164 signal candidates with 3.3% background (40 times more statistics than previous experiments<sup>17</sup>). This decay and its normalization channel ( $K^\pm \rightarrow \pi^\pm \pi^0$ ) were collected through the neutral trigger chain intended for the collection of  $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$  decays and therefore suffered from a very low trigger efficiency ( $\approx 50\%$ ). Elaborate studies were performed to measure these efficiencies and correct for them (see Fig. 2 (left)). The reconstructed  $M_{\gamma\gamma}$  spectrum can be seen in Fig. 2 for selected candidates (crosses), signal MC (yellow) and background (red).

The model dependent branching ratio of  $K^\pm \rightarrow \pi^\pm \gamma\gamma$  has been measured, assuming the validity of the  $O(p^6)$  ChPT as presented in<sup>16</sup> and taking  $\hat{c} = 2^a$ . The preliminary result is  $BR(K^\pm \rightarrow \pi^\pm \gamma\gamma) = (1.07 \pm 0.04_{stat} \pm 0.08_{syst}) \times 10^{-6}$ . A model independent BR measurement is in preparation, together with the extraction of  $\hat{c}$  from a fit to  $M_{\gamma\gamma}$  and BR.

#### 5 $K^\pm \rightarrow \pi^\pm \gamma e^+ e^-$ analysis

This decay is similar to  $K^\pm \rightarrow \pi^\pm \gamma\gamma$  with one photon internally converting into a pair of electrons. NA48/2 has reported the first observation of the decay  $K^\pm \rightarrow \pi^\pm \gamma e^+ e^-$  using the full 2003 and 2004 data sample<sup>18</sup>. 120 candidates with  $7.3 \pm 1.7$  estimated background events have been selected in the accessible region with  $M_{\gamma ee} > 0.26 \text{ GeV}/c^2$  invariant mass. The candidates are shown in Fig. 3 (left). Using  $K^\pm \rightarrow \pi^\pm \pi_D^0$  as normalization channel, the branching ratio has been determined in a model independent way to be  $BR = (1.19 \pm 0.12_{stat} \pm 0.04_{syst}) \times 10^{-8}$  for  $M_{\gamma ee} > 0.26 \text{ GeV}/c^2$ . The parameter  $\hat{c}$  has also been measured assuming the validity of  $O(p^6)$ <sup>19</sup> and found to be  $\hat{c} = 0.90 \pm 0.45$ .

<sup>a</sup>This is a realistic assumption based on previous results by<sup>17</sup> which obtained  $\hat{c} = 1.8 \pm 0.6$ .

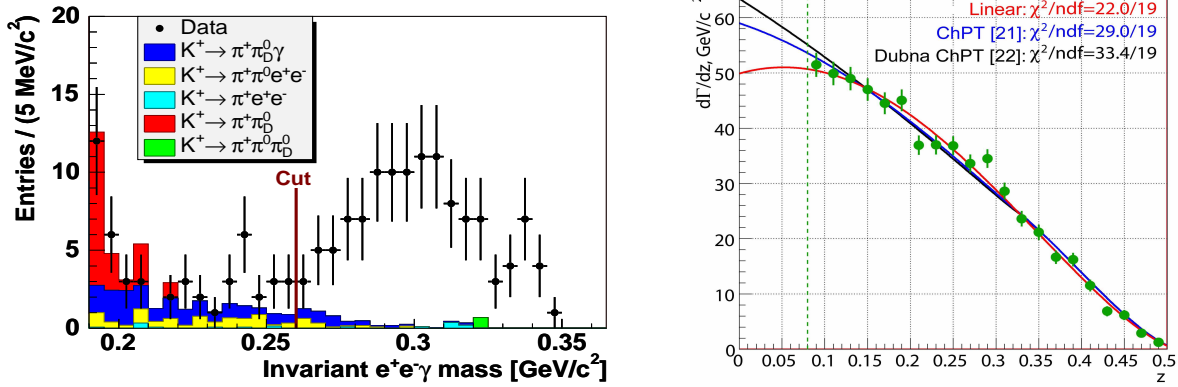


Figure 3: (Left)  $M_{\gamma e^+e^-}$  invariant mass of  $K^\pm \rightarrow \pi^\pm \gamma e^+e^-$  candidates. Crosses are signal and colored histograms background. (Right)  $K^\pm \rightarrow \pi^\pm e^+e^-$  differential decay rate and different fit results from the considered models.

## 6 $K^\pm \rightarrow \pi^\pm e^+e^-$ analysis

The FCNC process  $K^\pm \rightarrow \pi^\pm e^+e^-$  can be described in ChPT<sup>20</sup>. NA48/2 has collected 7146 candidates with 0.6% background. The decay rate has been measured using  $K^\pm \rightarrow \pi^\pm \pi_D^0$  as normalization. A preliminary model independent measurement for  $z = M_{e^+e^-}^2/M_{K^\pm}^2 > 0.08$  gave  $BR = (2.26 \pm 0.03_{stat} \pm 0.03_{syst} \pm 0.06_{ext}) \times 10^{-7}$ . Model dependent fits to the  $z$ -spectrum have been performed (Fig. 3 (right)), obtaining the corresponding form factors and BR. The preliminary average BR in the full kinematic range is:  $BR = (3.08 \pm 0.04_{stat} \pm 0.08_{ext} \pm 0.07_{model}) \times 10^{-7}$ . Comparison of results with previous experiments and theoretical predictions can be found in<sup>23</sup>.

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